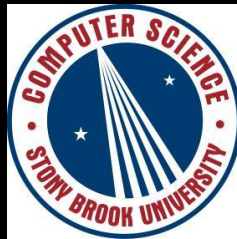


# What is Strange in Large Networks?

## Graph-based Irregularity and Fraud Detection

Leman Akoglu



Christos Faloutsos

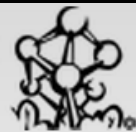


Carnegie  
Mellon  
University



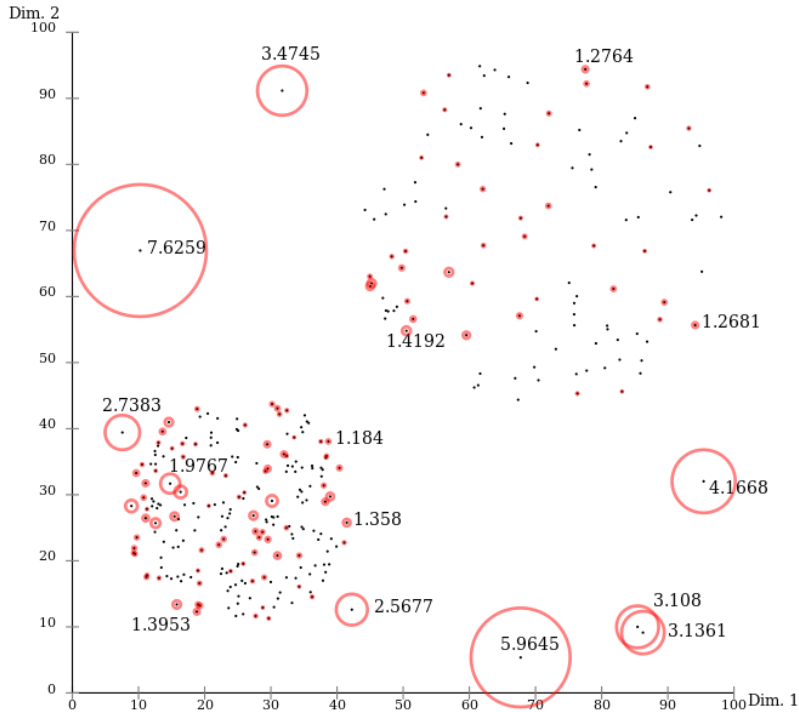
**IEEE**  
**ICDM**

**International Conference on Data Mining**  
**Brussels 10-13 Dec 2012**

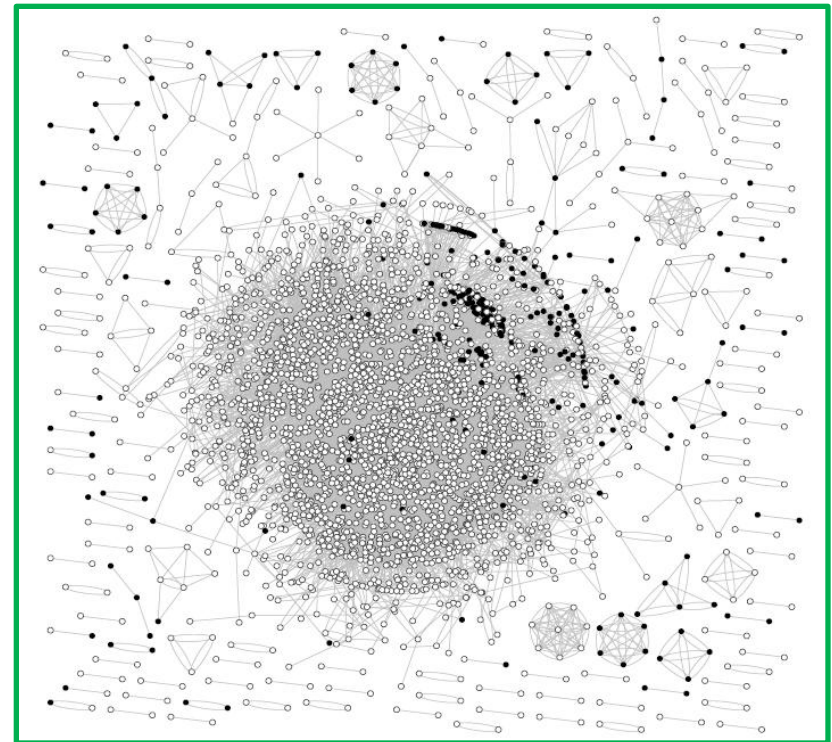


# Outliers vs. Graph anomalies

This tutorial



Clouds of points  
(multi-dimensional)



Inter-linked objects  
(network)

# Roadmap

13:30 Introduction & motivation

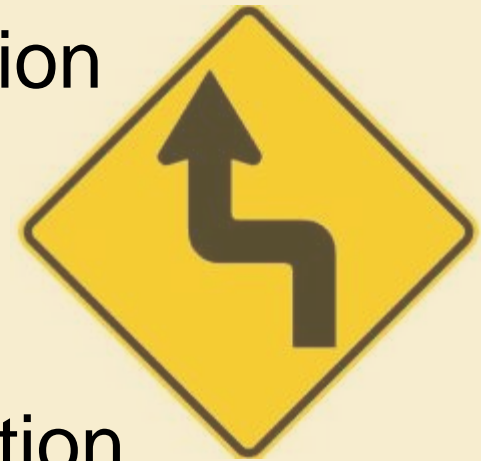
**Part I:** Anomaly detection  
in static data

15:30 **Coffee break**

16:00 **Part II:** Anomaly detection  
in dynamic data

**Part III:** Graph-based algorithms  
& applications

18:00 The End



# Disclaimers

This tutorial does not necessarily cover all related work



References are not necessarily authoritative and complete

Several slides have been reused or modified by the permission of the original creators.

# Anomaly detection: Applications

## Tax evasion



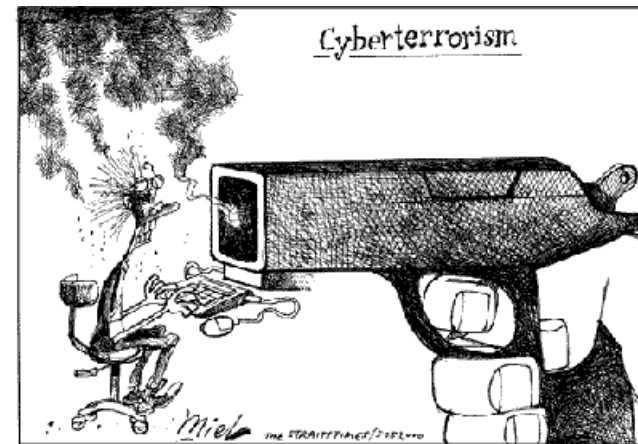
## Credit card fraud



## Healthcare fraud



## Network intrusion



# Applications

Investment fraud      Click fraud      Malware

Insurance fraud      Malicious cargo      Spyware

Auction fraud      Damage detection

Fake reviews      Medical diagnosis      Email spam

False advertising

Performance monitoring

Web spam      Insider threat

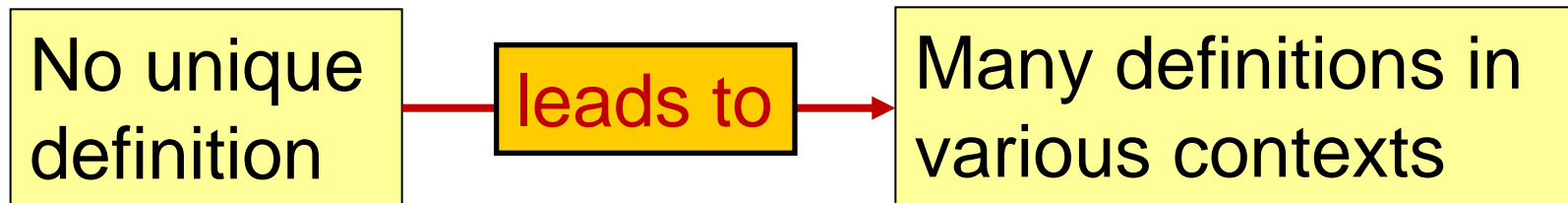
Image/video surveillance



# Anomaly detection: definition

- (Hawkins' Definition of Outlier, 1980)

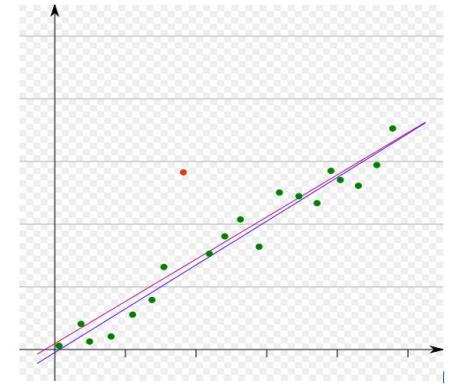
“An outlier is an observation that differs so much from other observations as to arouse suspicion that it was generated by a different mechanism.”



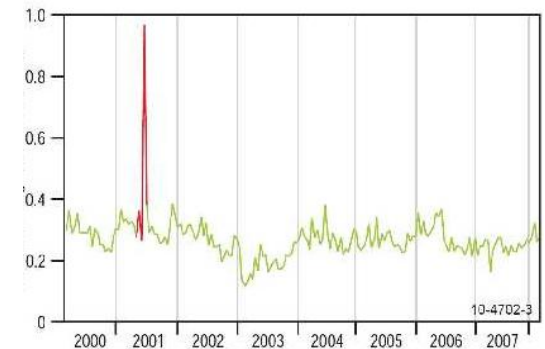
outlier, anomaly, outbreak, event, fraud, ...

# Anomaly detection: definition

- for **practical** purposes,
  - a **record/point/graph-node/graph-edge** is flagged as **anomalous** if a **rarity/likelihood/outlierness** score exceeds a user-defined threshold

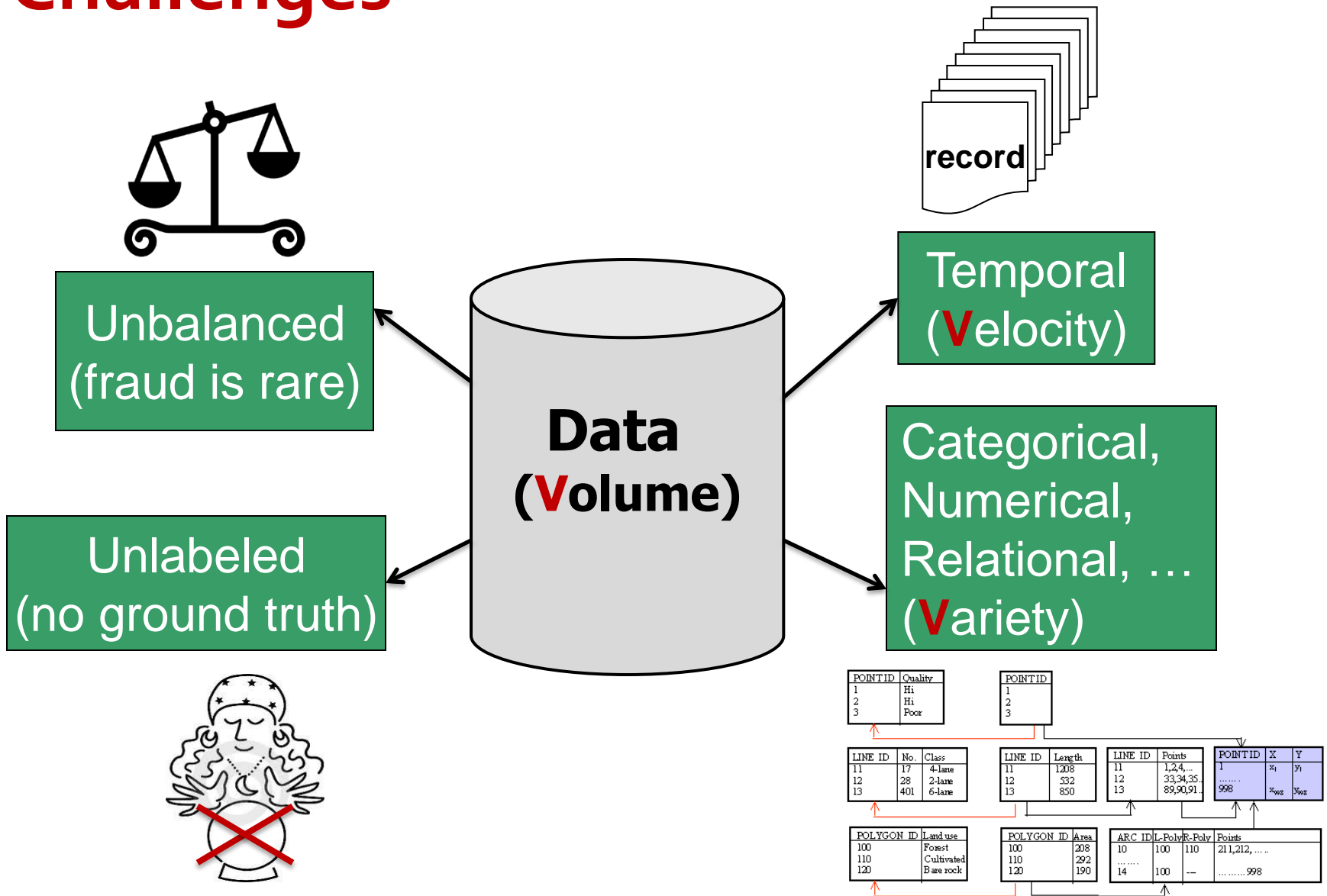


- **anomalies:**
  - → **rare** (e.g., rare combination of categorical attribute values)
  - → **isolated** points in n-d spaces
  - → **surprising** (don't fit well in our mental/statistical model == need too many bits under MDL)





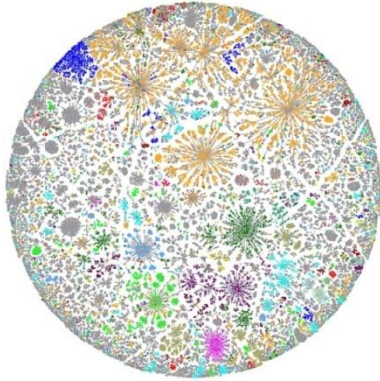
# Challenges



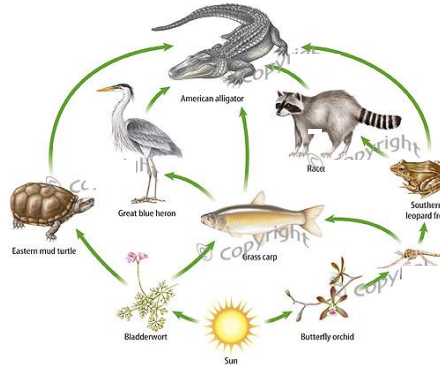
# Why graph-based detection?

- Powerful representation
  - Interdependent instances
  - Long-range relations
  - Node/Edge attributes (data complexity)
  - Hard to fake/alter (adversarial robustness)
  
- Abundant relational data
  - Web, email, phone call, ...

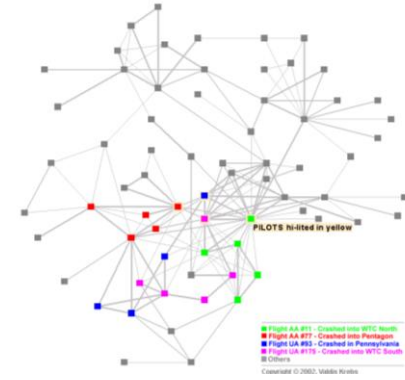
# Real graphs (1)



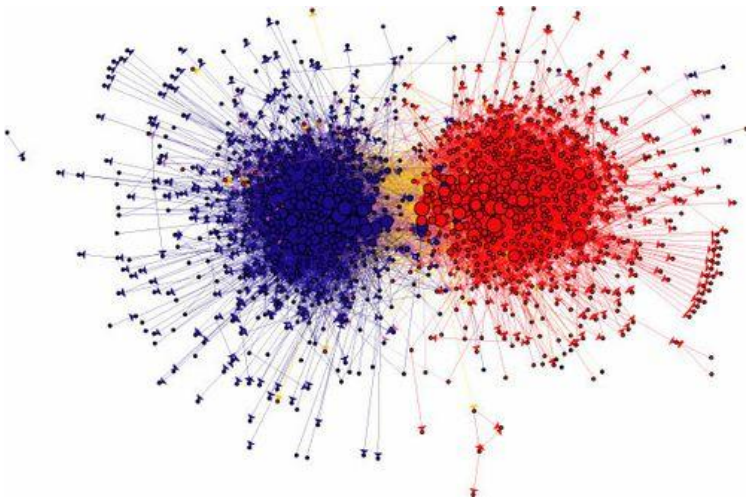
Internet Map



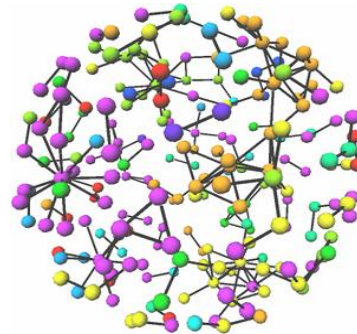
Food Web



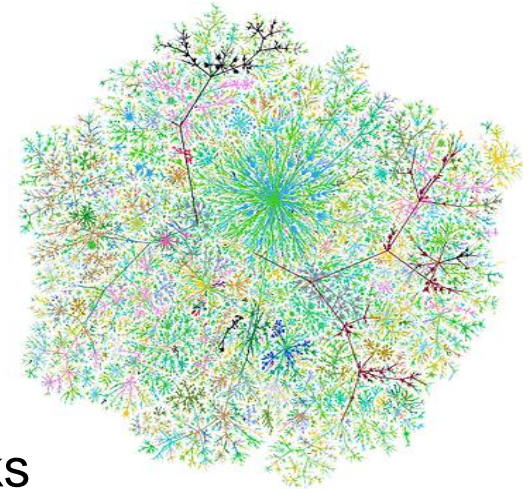
Terrorist Network



Blog networks

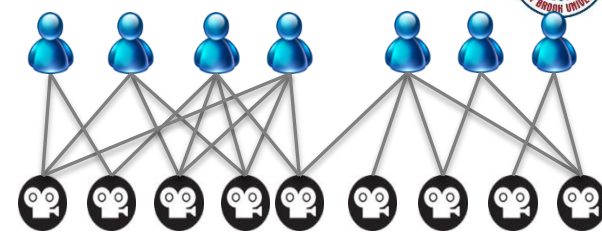


Biological networks

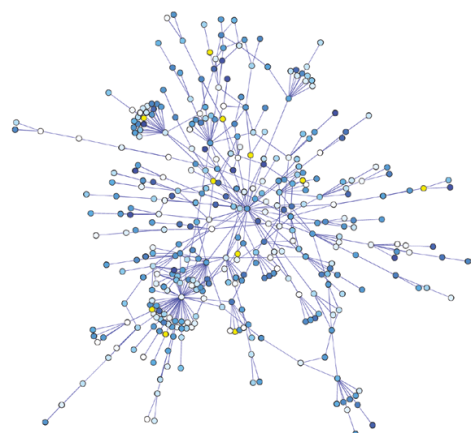


Web Graph

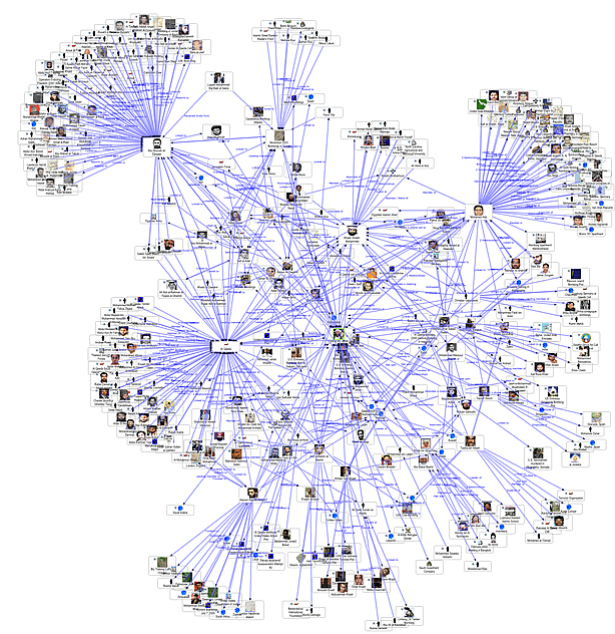
# Real graphs (2)



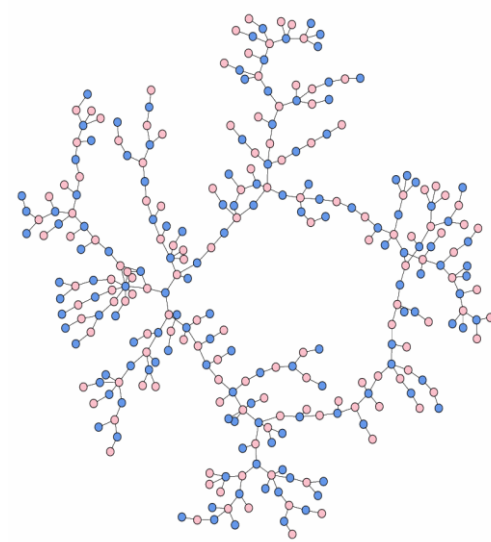
Retail networks



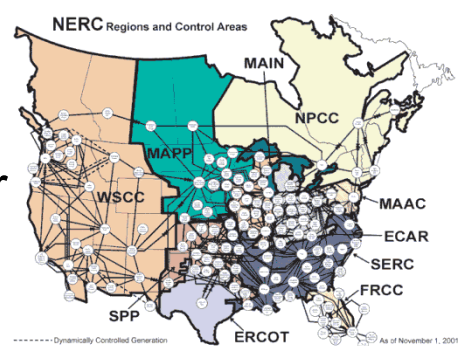
Protein-protein Interaction



Social Network



Dating network

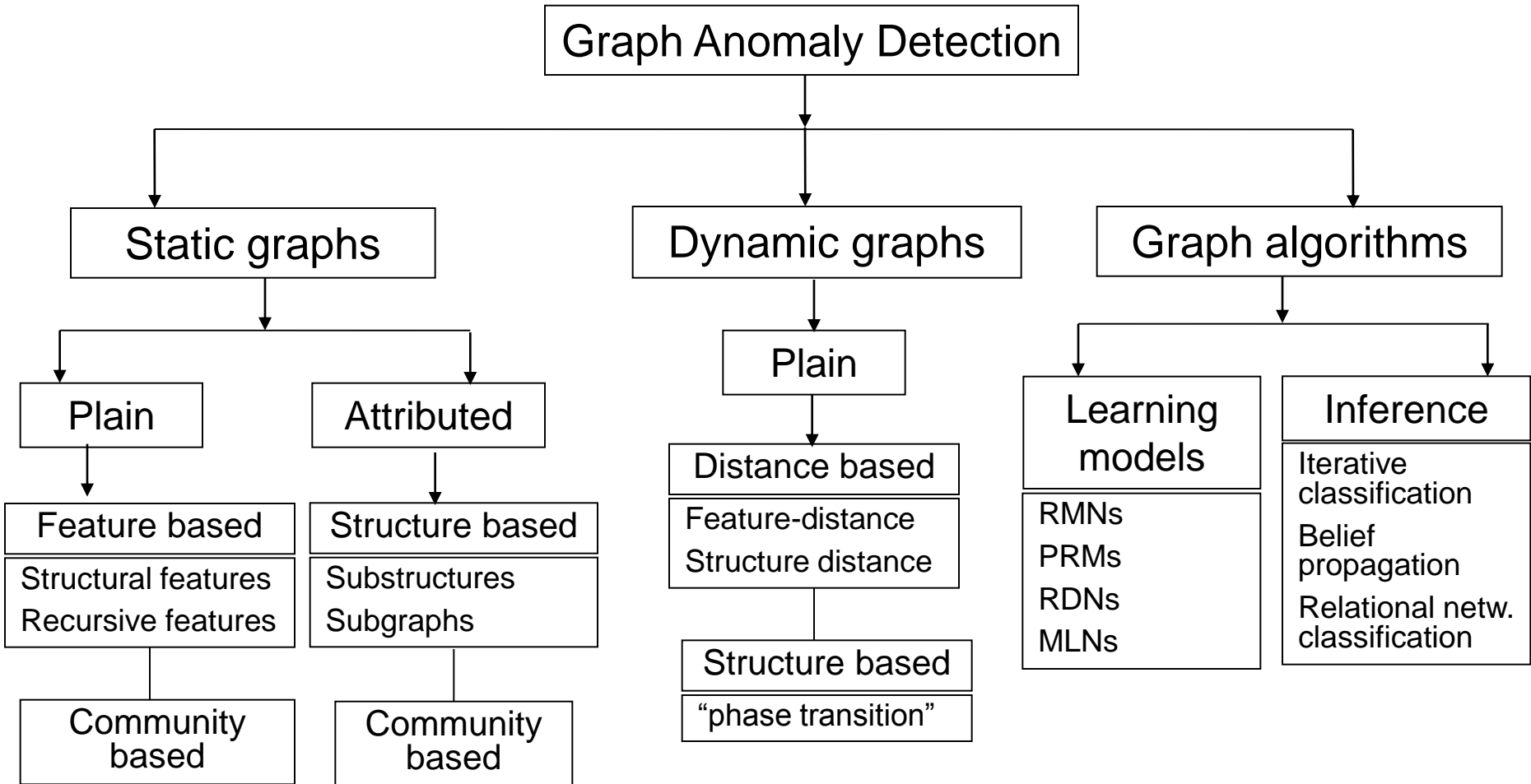


Power Grid

# Problem revisited for graphs

- Three different problem settings
  - Unlabeled/Labeled (Attributed) Graphs
  - Static/Dynamic Graphs
  - Un-/Semi-/- Supervised Graph Techniques

# Taxonomy



# Goal of this tutorial

- Introduce various **problem formulations**
  - Definitions change by application/representation
- **Applications** of problem settings
  - Intrusion, fraud, spam
- Introduce existing **techniques**
  - Model fitting, factorization, relational inference
- **Pros and Cons**
  - Parameters, scalability, robustness

# Tutorial Outline

- Motivation, applications, challenges
- ➔ **Part I:** Anomaly detection in **static** data
  - Overview: Outliers in **clouds of points**
  - Anomaly detection in **graph data**
- **Part II:** Event detection in **dynamic** data
  - Overview: Change detection in **time series**
  - Event detection in **graph sequences**
- **Part III:** Graph-based **algorithms and apps**
  - Algorithms: **relational learning**
  - Applications: **fraud and spam** detection



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# **Part I: Anomaly detection in static graphs**

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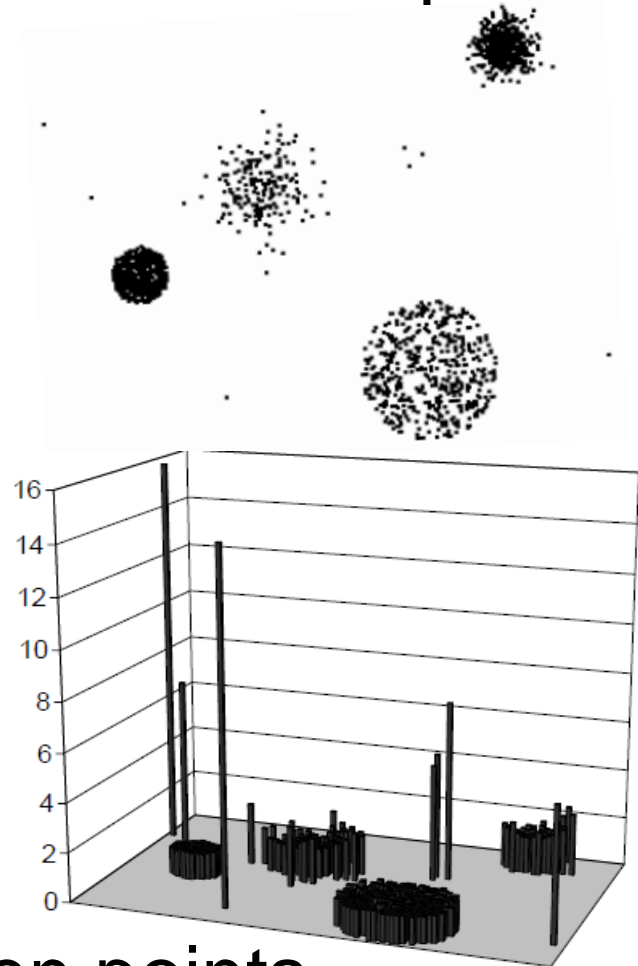
# Part I: Outline

- ➔ Overview: Outliers in **clouds of points**
  - ❑ Outliers in **numerical** data points
    - distance-based, density-based, ...
  - ❑ Outliers in **categorical** data points
    - model-based
- Anomaly detection in **graph data**
  - ❑ Anomalies in unlabeled, **plain** graphs
  - ❑ Anomalies in node-/edge-labeled, **attributed** graphs

# Outlier detection

## ■ Anomalies in multi-dimensional data points

- ❑ Density-based
- ❑ Distance-based
- ❑ Depth-based
- ❑ Distribution-based
- ❑ Clustering-based
- ❑ Classification-based
- ❑ Information theory-based
- ❑ Spectrum-based
- ❑ ...



## ■ No relational links between points

# Part I: References (outliers)

- M. M. Breunig, H.-P. Kriegel, R. T. Ng, and J. Sander. [LOF: Identifying density-based local outliers](#). SIGMOD, 2000.
- S. Papadimitriou, H. Kitagawa, P. B. Gibbons, and C. Faloutsos. [LOCI: Fast outlier detection using the local correlation integral](#). ICDE, 2003.
- C. C. Aggarwal and P. S. Yu. [Outlier detection for high dimensional data](#). SIGMOD, 2001.
- A. Ghoting, S. Parthasarathy and M. Otey, [Fast Mining of Distance Based Outliers in High-Dimensional Datasets](#). DAMI, 2008.
- Y. Wang, S. Parthasarathy and S. Tatikonda, [Locality Sensitive Outlier Detection](#). ICDE, 2011.
- Kaustav Das, Jeff Schneider. [Detecting Anomalous Records in Categorical Datasets](#). KDD 2007.

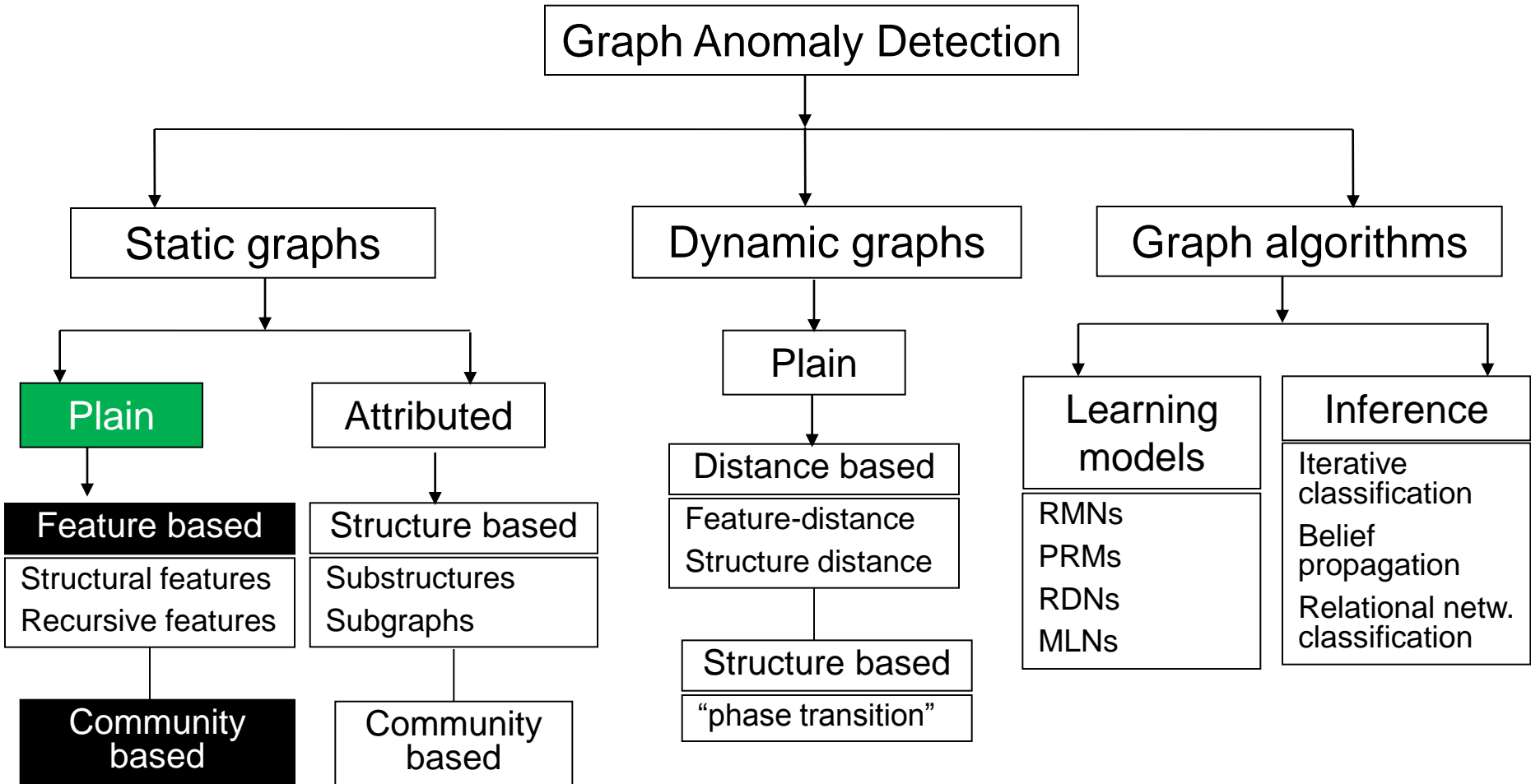
# Part I: References (outliers)

- Müller E., Schiffer M., Seidl T. [Adaptive Outlierness for Subspace Outlier Ranking](#). CIKM, 2010.
- Müller E., Assent I., Iglesias P., Mülle Y., Böhm K. [Outlier Ranking via Subspace Analysis in Multiple Views of the Data](#). ICDM, 2012.
- L. Akoglu, H. Tong, J. Vreeken, and C. Faloutsos. [Fast and Reliable Anomaly Detection in Categorical Data](#). CIKM, 2012.
- A. Chaudhary, A. S. Szalay, and A. W. Moore. [Very fast outlier detection in large multidimensional data sets](#). DMKD, 2002.
- **Survey: V. Chandola, A. Banerjee, V. Kumar: [Anomaly Detection: A Survey](#). ACM Computing Surveys, Vol. 41(3), Article 15, July 2009.**

# Part I: Outline

- Overview: Outliers in **clouds of points**
  - Outliers in **numerical** data points
    - distance-based, density-based, ...
  - Outliers in **categorical** data points
    - model-based
- Anomaly detection in **graph data**
  - ➔ Anomalies in unlabeled, **plain** graphs
    - Anomalies in node-/edge-labeled, **attributed** graphs

# Taxonomy



# Anomalies in Weighted Graphs

## ■ Problem:

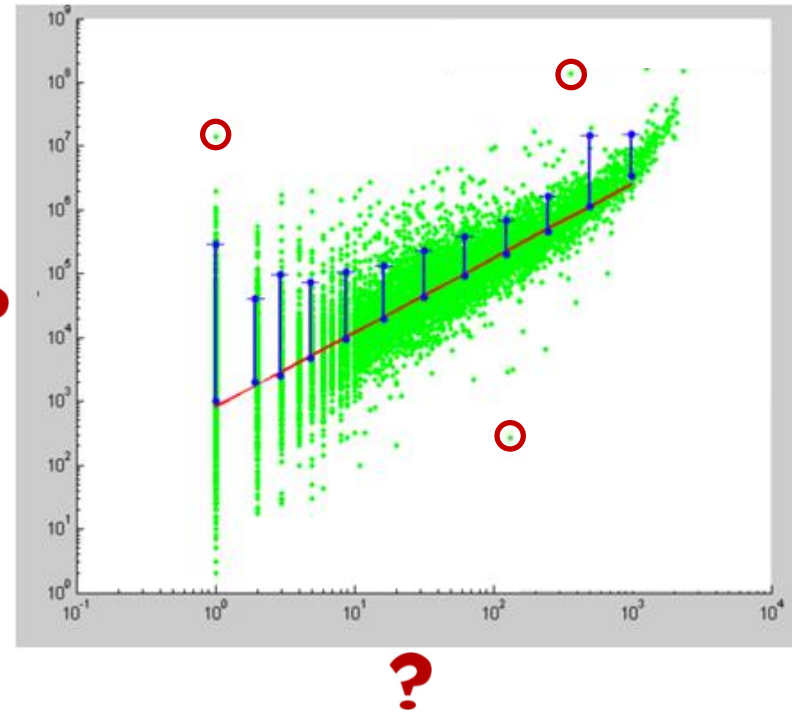
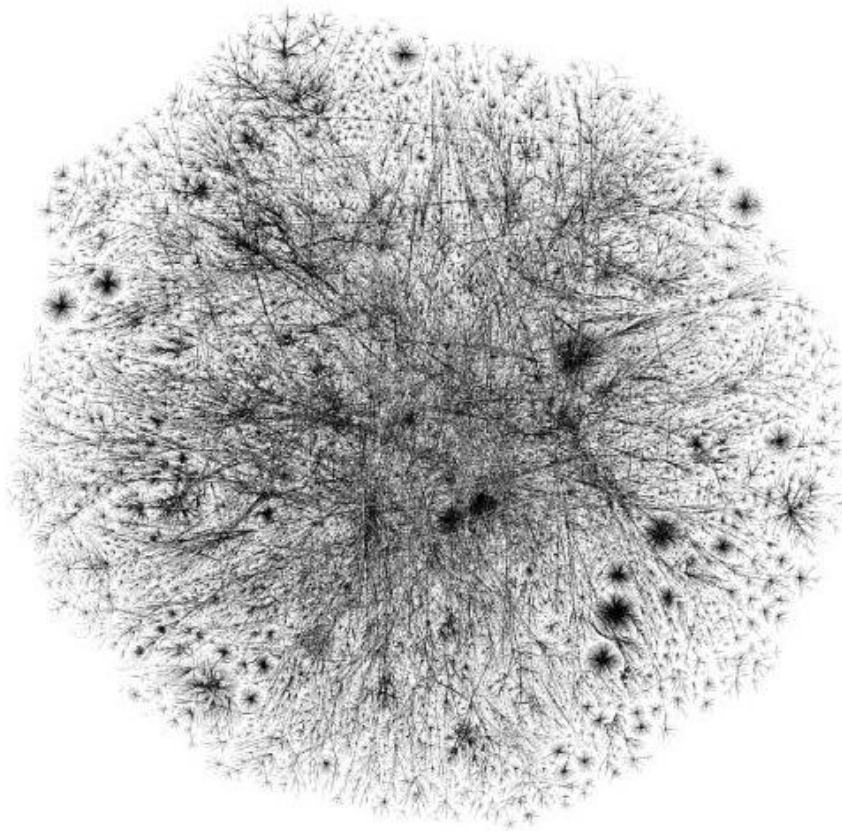
Q1. Given a **weighted** and **unlabeled** graph, how can we spot **strange, abnormal, extreme** nodes?

Q2. Can we **explain why** the spotted nodes are anomalous?





# Problem sketch

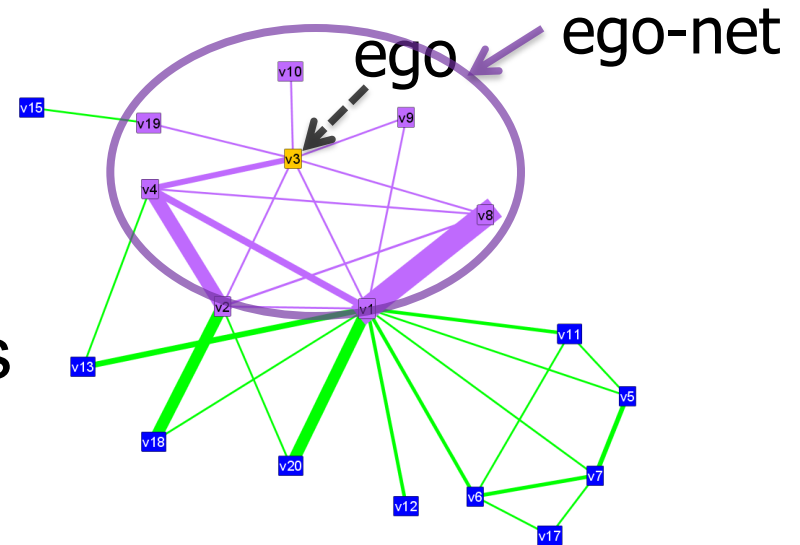


# OddBall: approach

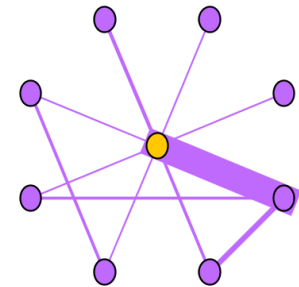
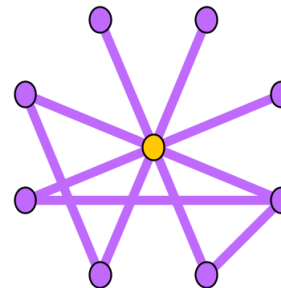
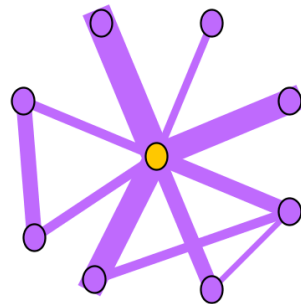
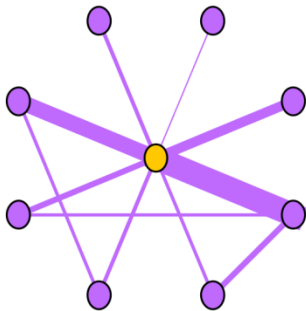
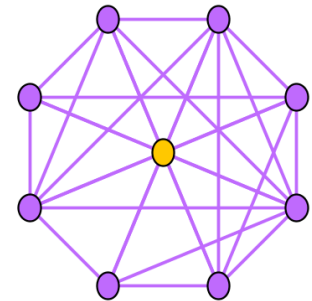
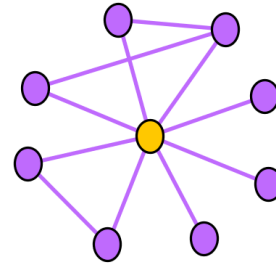
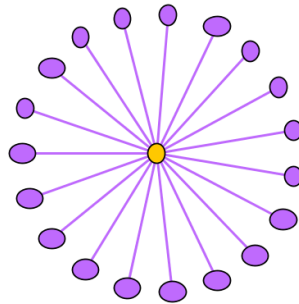
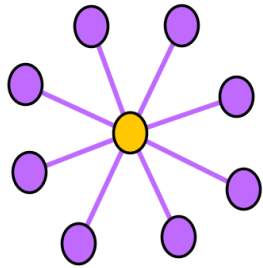
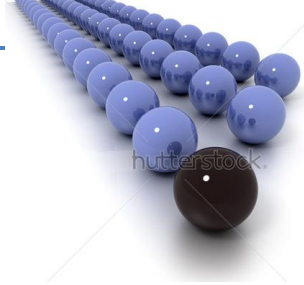
- 1) For each node,
  - 1.1) Extract “ego-net” (=1-step neighborhood)
  - 1.2) Extract **features** (#edges, total weight, etc.)
    - features that could yield “laws”
    - features **fast to compute** and interpret

- 2) Detect **patterns**:
  - regularities

- 3) Detect **anomalies**:
  - “distance” to patterns

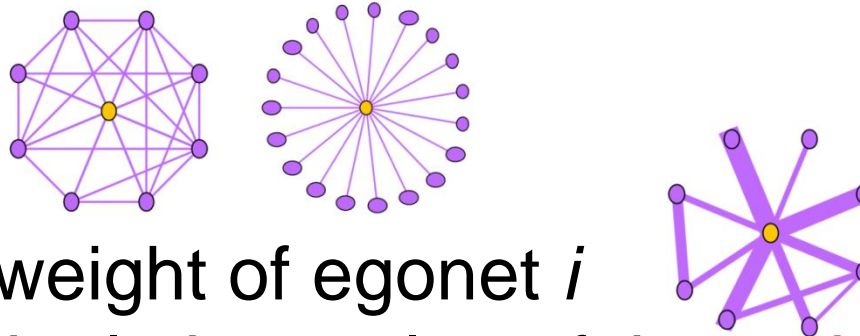


# What is odd?

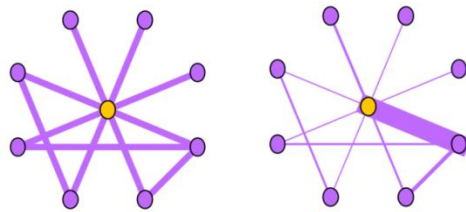


# Which features to compute?

- $N_i$ : number of neighbors (degree) of ego  $i$
- $E_i$ : number of edges in egonet  $i$

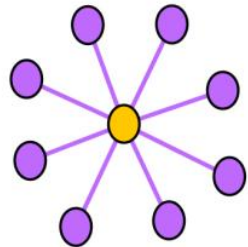


- $W_i$ : total weight of egonet  $i$
- $\lambda_{w,i}$ : principal eigenvalue of the **weighted** adjacency matrix of egonet  $i$

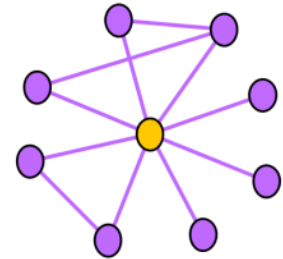


# Weighted principal eigenvalue

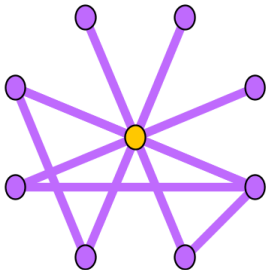
details



$$\lambda_{w,i} = \sqrt{N} = \sqrt{E} = \sqrt{W}$$

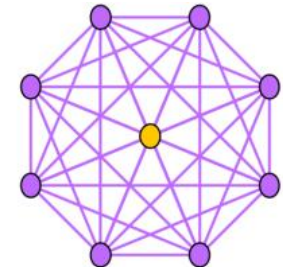


$$\lambda_{w,i} > \sqrt{N} \\ \propto \sqrt{E}, \sqrt{W}$$



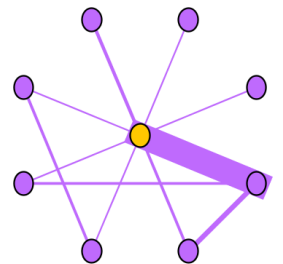
$$\lambda_{w,i} \propto \sqrt{W}$$

$$\lambda_{w,i} = N \approx \sqrt{W}$$



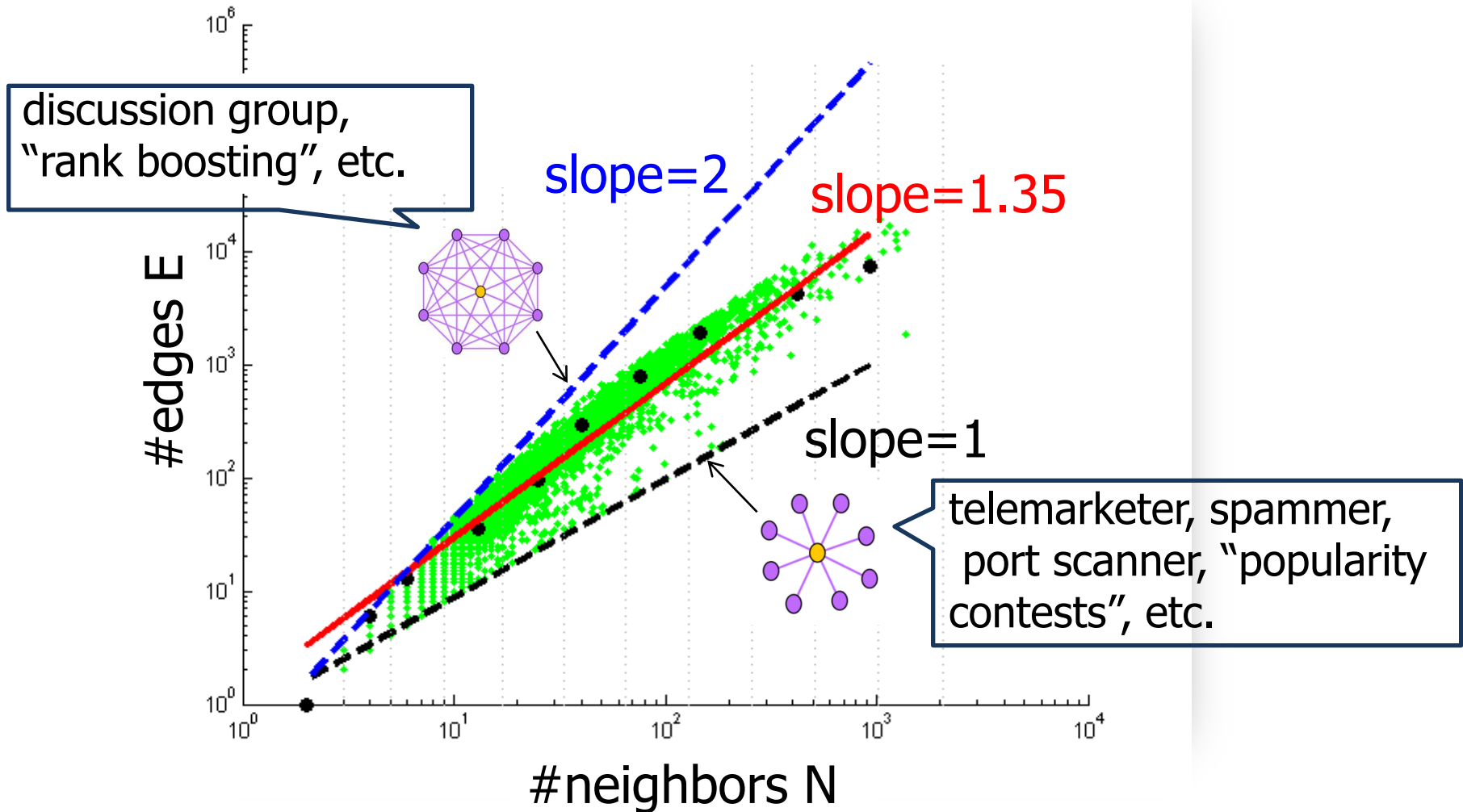
$$\lambda_{w,i} = W$$

$$\lambda_{w,i} \approx W$$

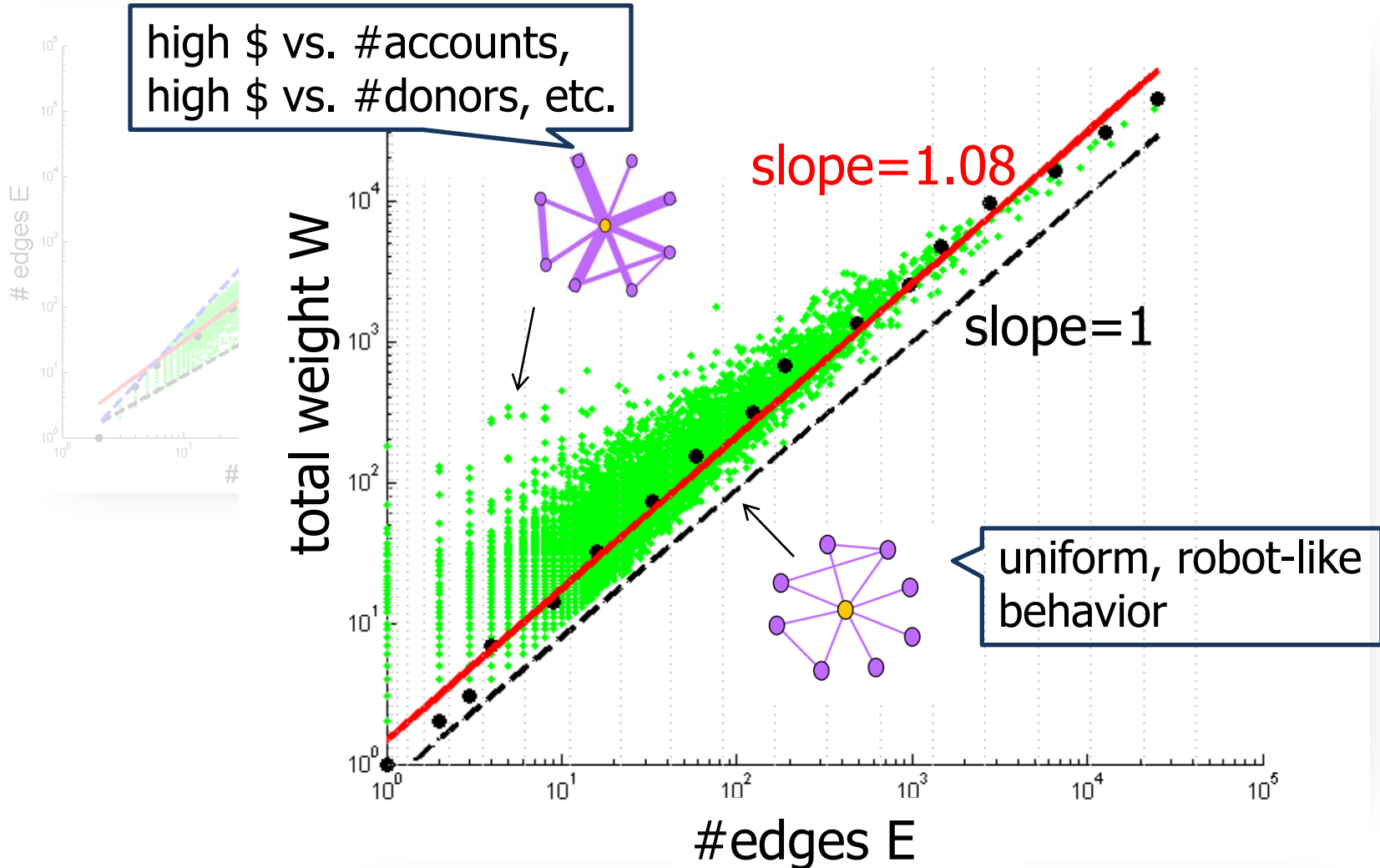


N: #neighbors, W: total weight

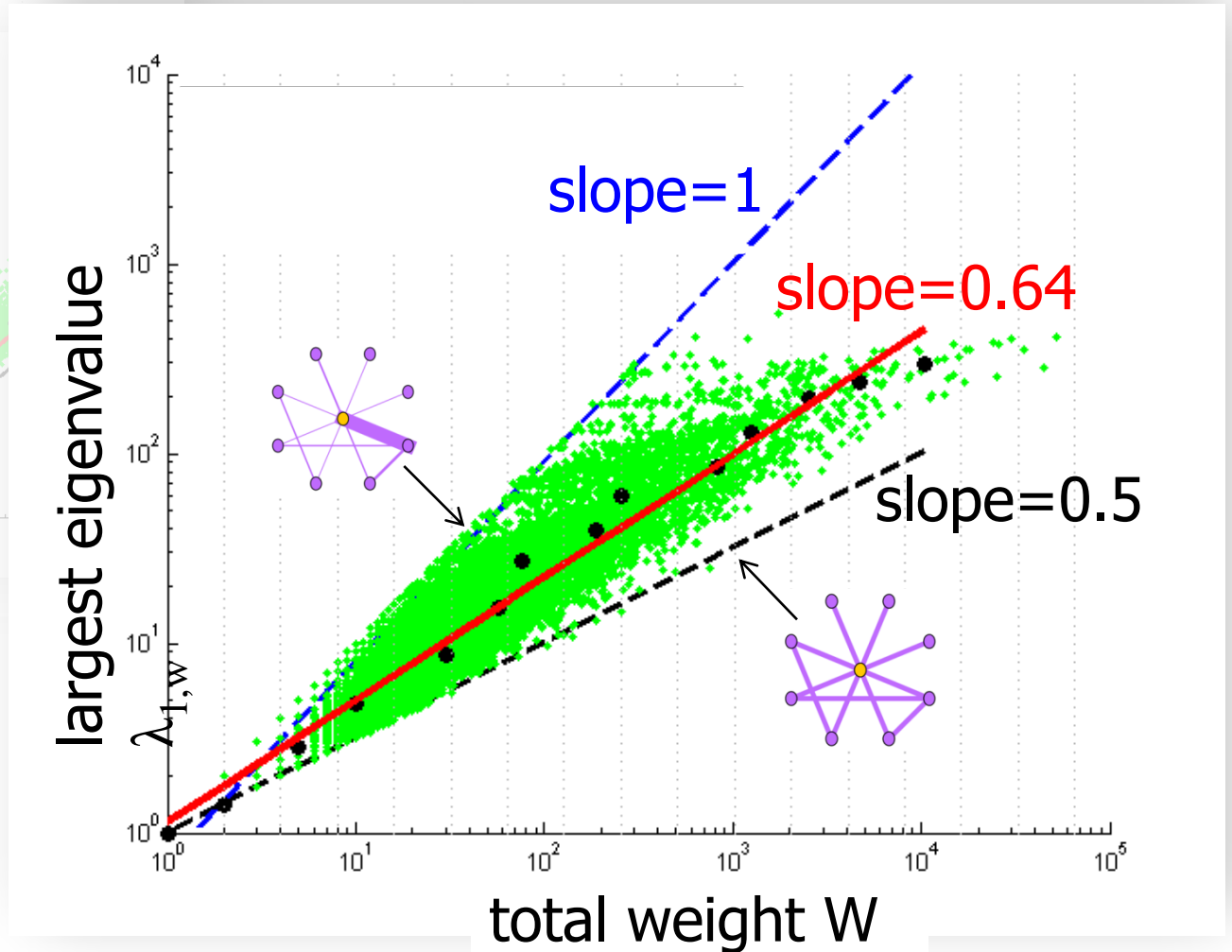
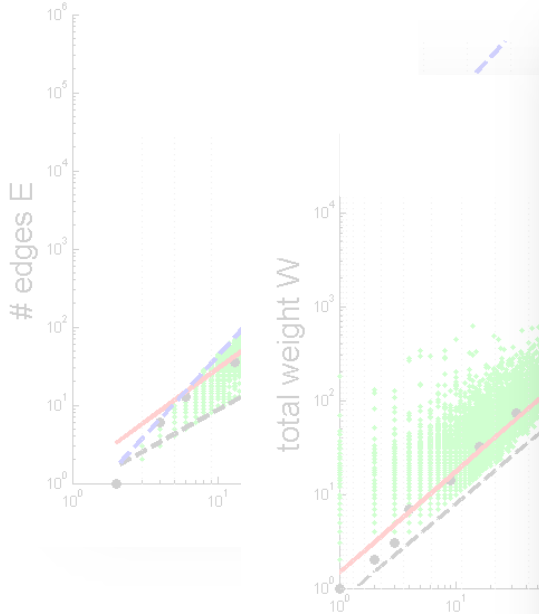
# OddBall: pattern#1



# OddBall: pattern#2



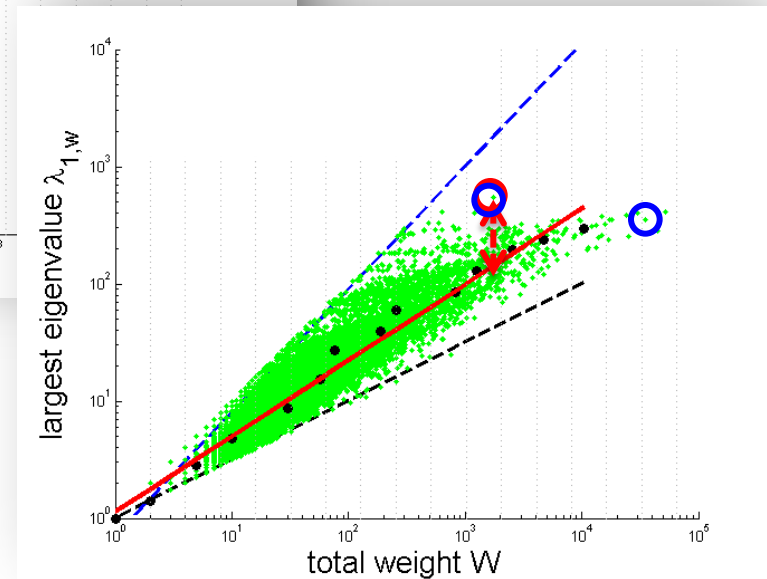
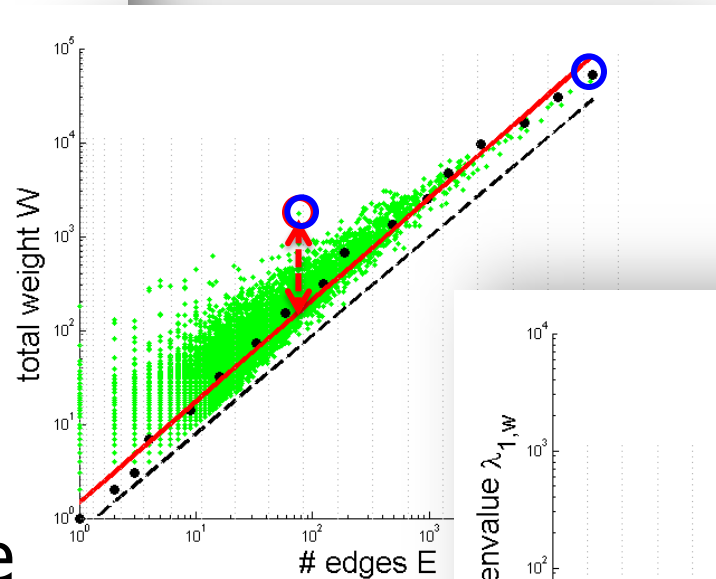
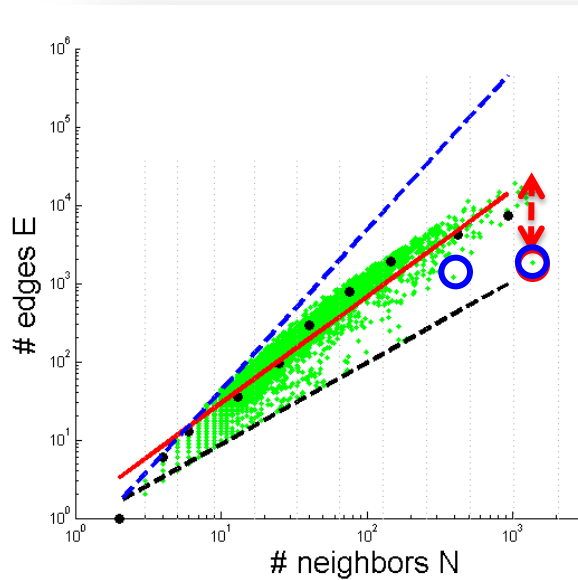
# OddBall: pattern#3





# OddBall: anomaly detection

$\text{score}_{\text{dist}}$  = distance to fitting line  
 $\text{score}_{\text{outl}}$  = outlier-ness score  
 $\text{score} = \text{func}(\text{score}_{\text{dist}}, \text{score}_{\text{outl}})$

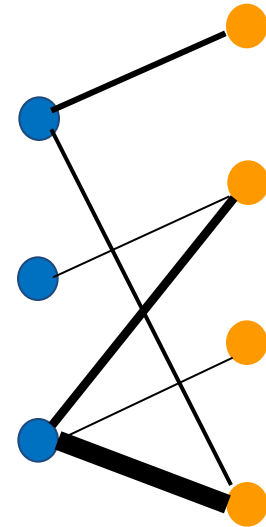


- ✓ can tell what type of anomaly a node belongs to
- ✓ can quantify "anomalous-ness" of nodes using score

# OddBall: datasets

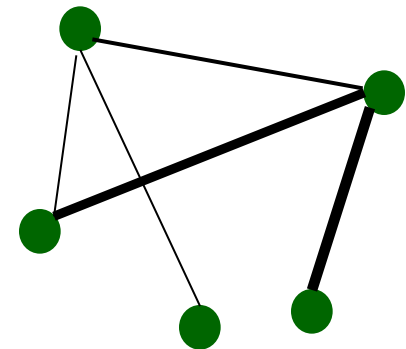
## Bipartite graphs:

	$ V $	$ E $
1. <b>FEC Don2Com</b>	1.6M	2M
2. <b>FEC Com2Cand</b>	6K	125K
3. <b>DBLP Auth2Conf</b>	21K	1M

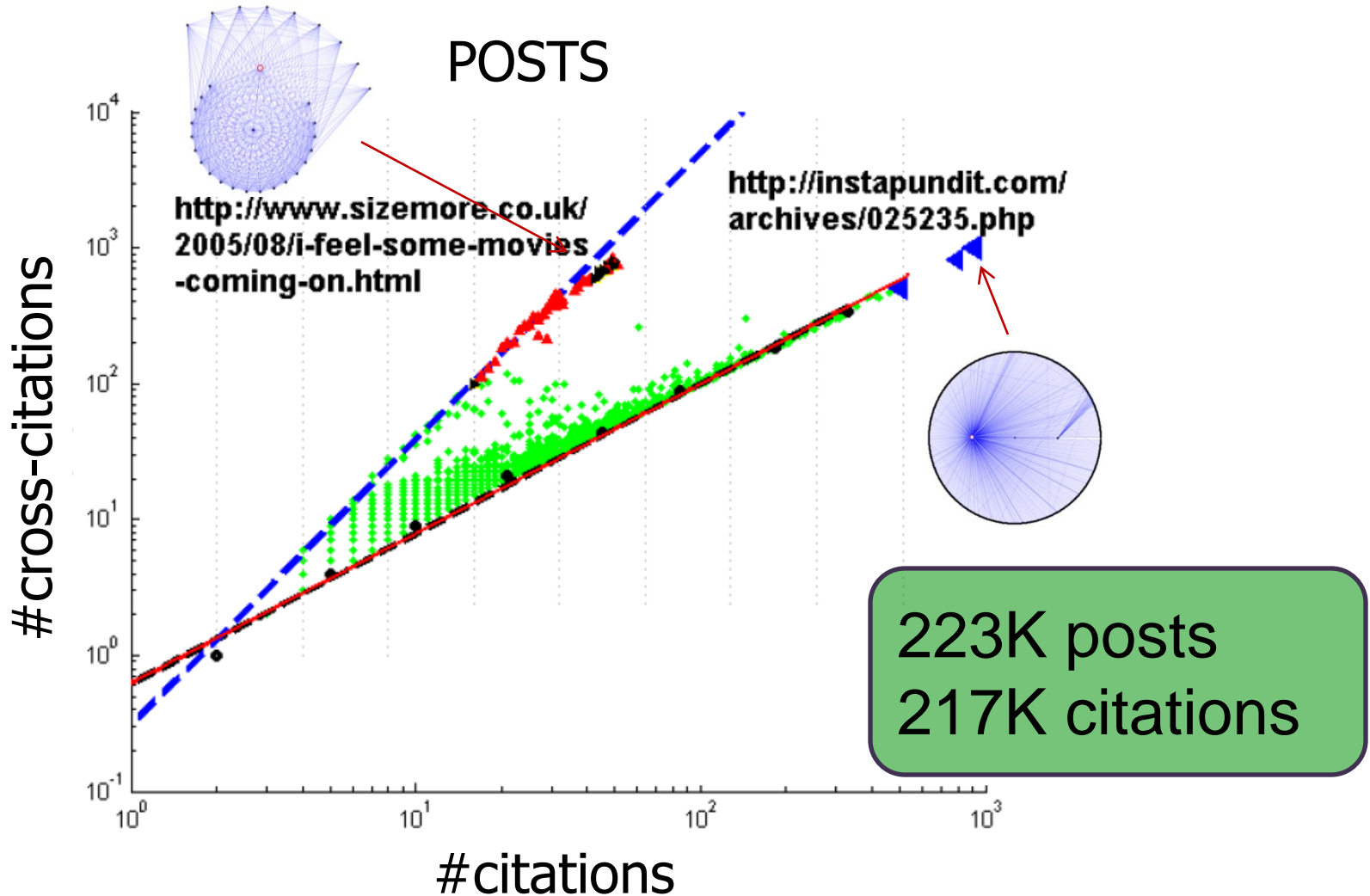


## Unipartite graphs:

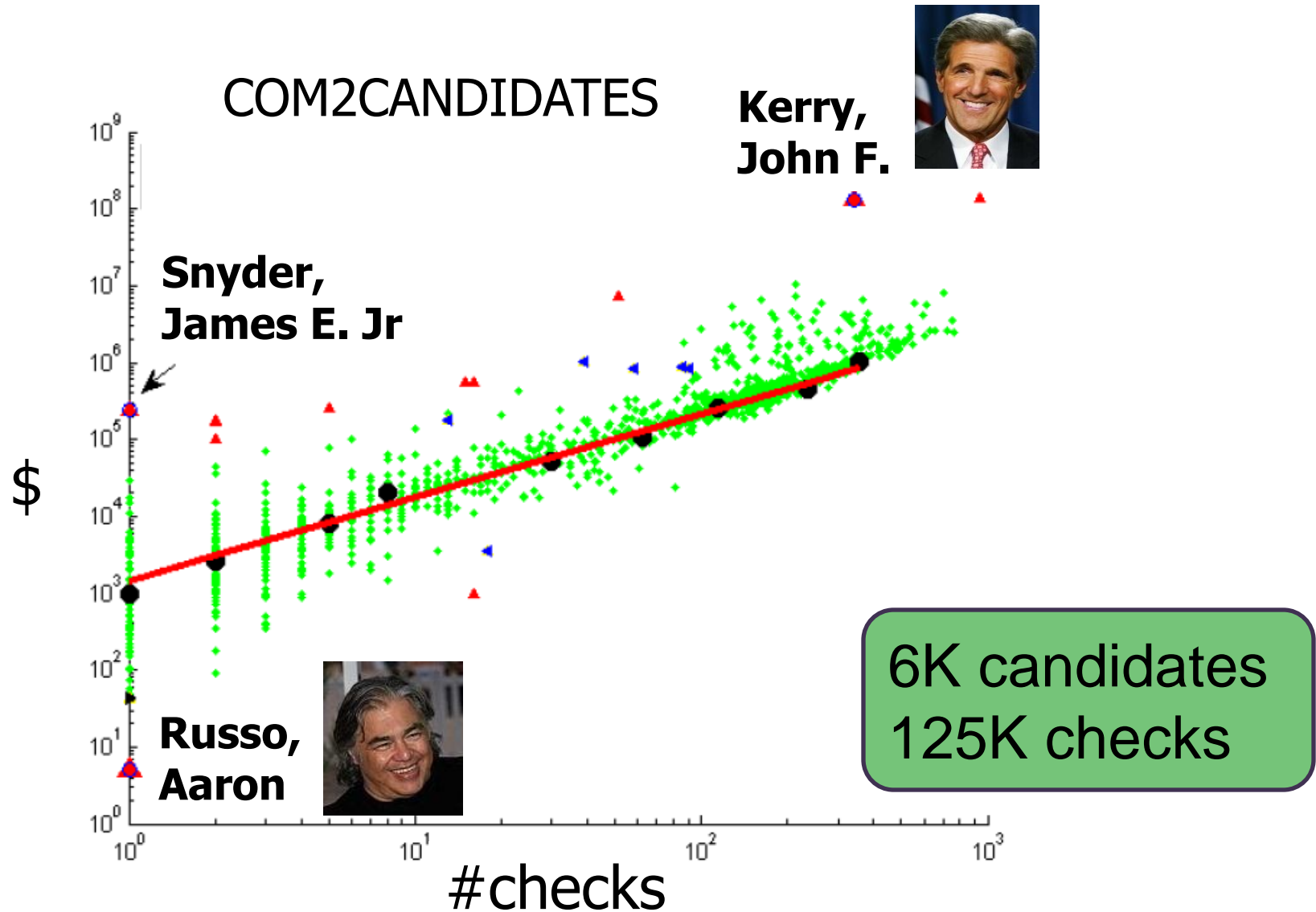
	$ V $	$ E $
4. <b>BlogNet</b>	27K	126K
5. <b>PostNet</b>	223K	217K
6. Enron	36K	183K
7. AS peering	11K	8K



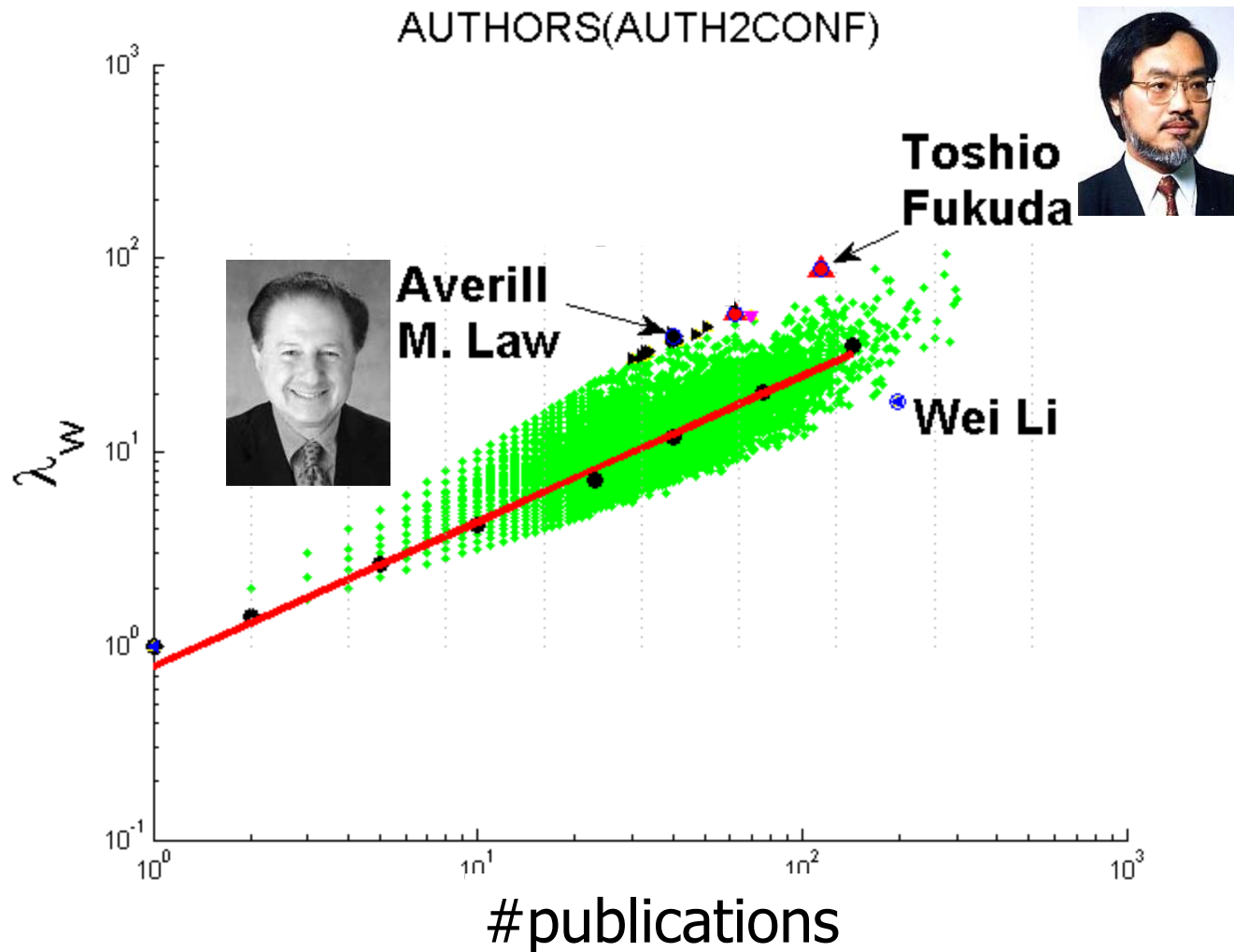
# OddBall at work (Posts)



# OddBall at work (FEC)

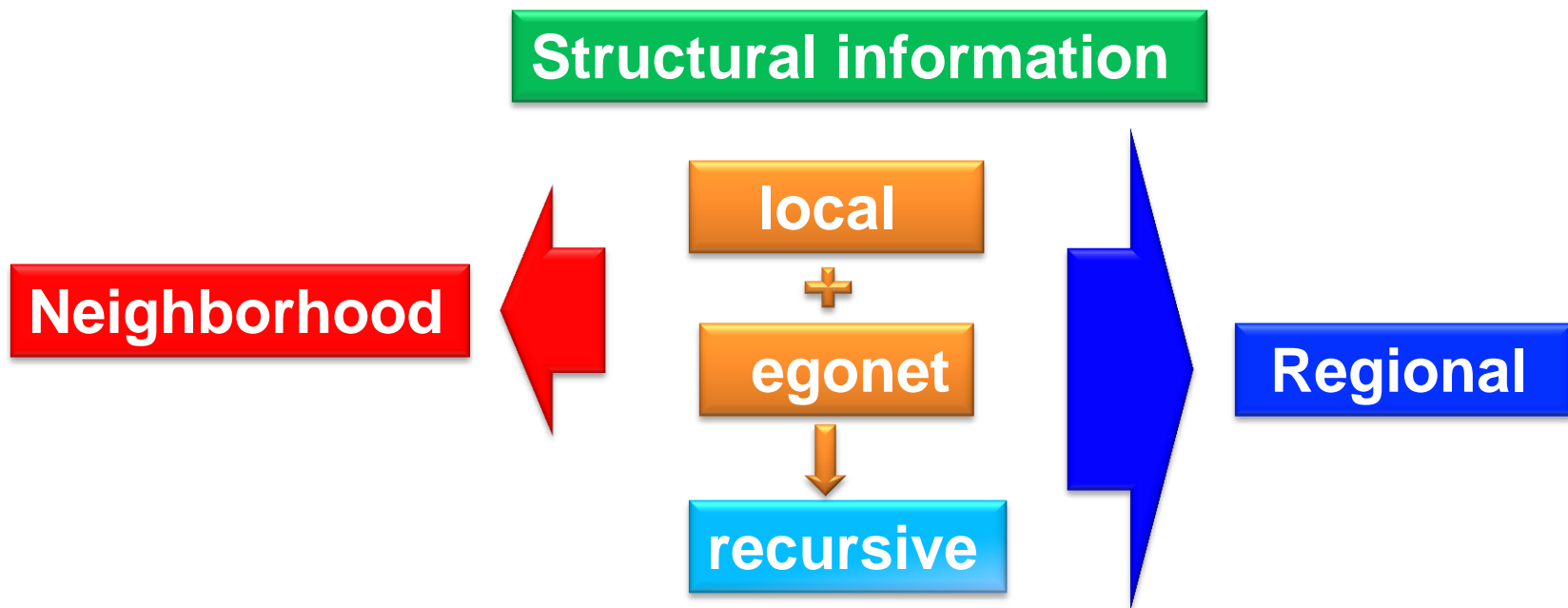


# OddBall at work (DBLP)



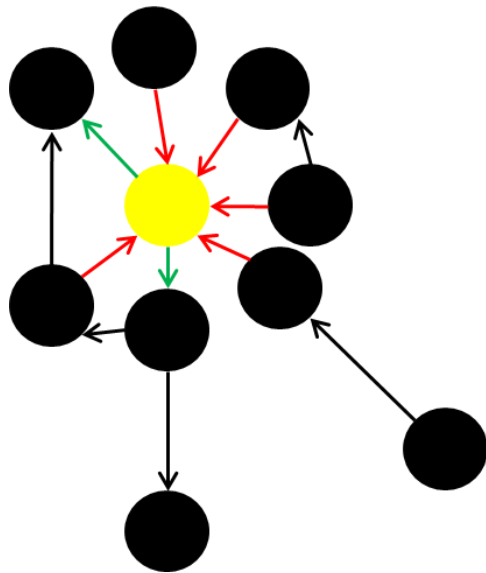
# Recursive structural features

- **Main idea:** recursively combine “local” (node-based) and neighbor (egonet-based) features
  - **Recursive feature:** any aggregate computed over any feature (including recursive) value among a node’s neighbors



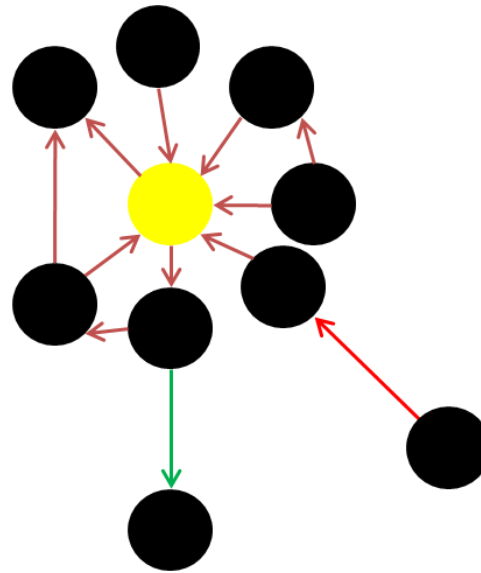
# Recursive structural features

local



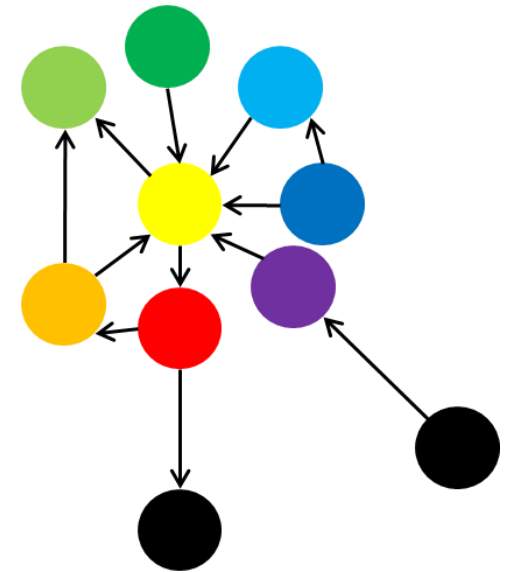
**in-** and **out-**degree,  
**weighted** versions

egonet



**within-**, **incoming-**,  
**outgoing-egonet**  
edges, **weighted**  
versions

recursive

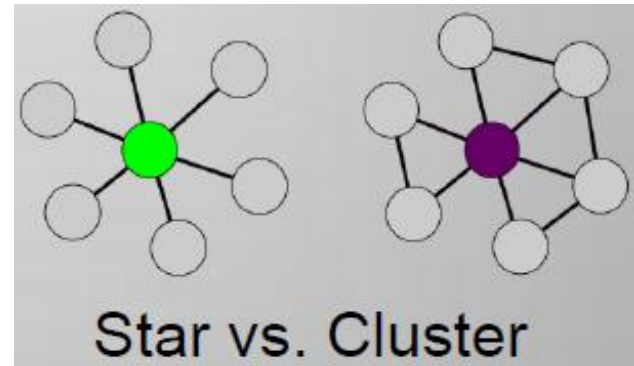
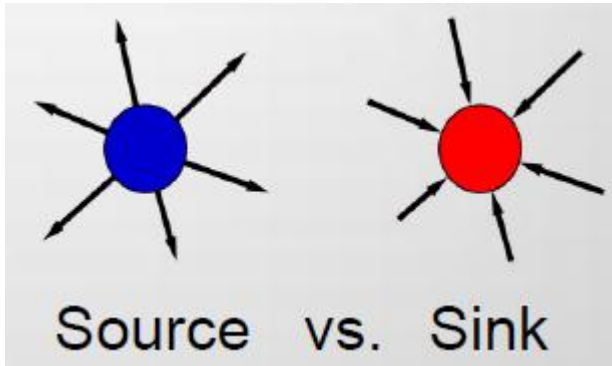


**aggregate** feature  
over neighbors  
e.g. max/min/avg degree

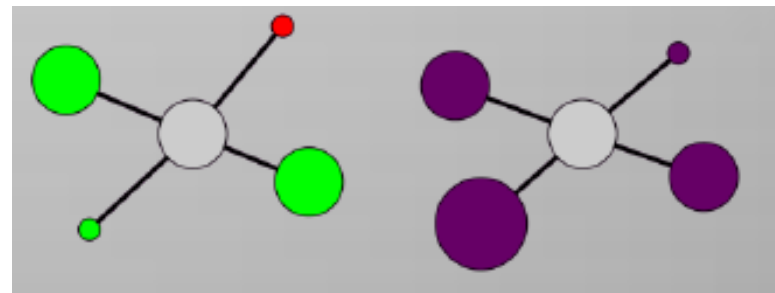
$$(1 + 1 + 2 + 0 + 1 + 0 + 1) / 7 = 0.86$$

# Recursive structural features

- **Neighborhood** features
  - captures node connectivity

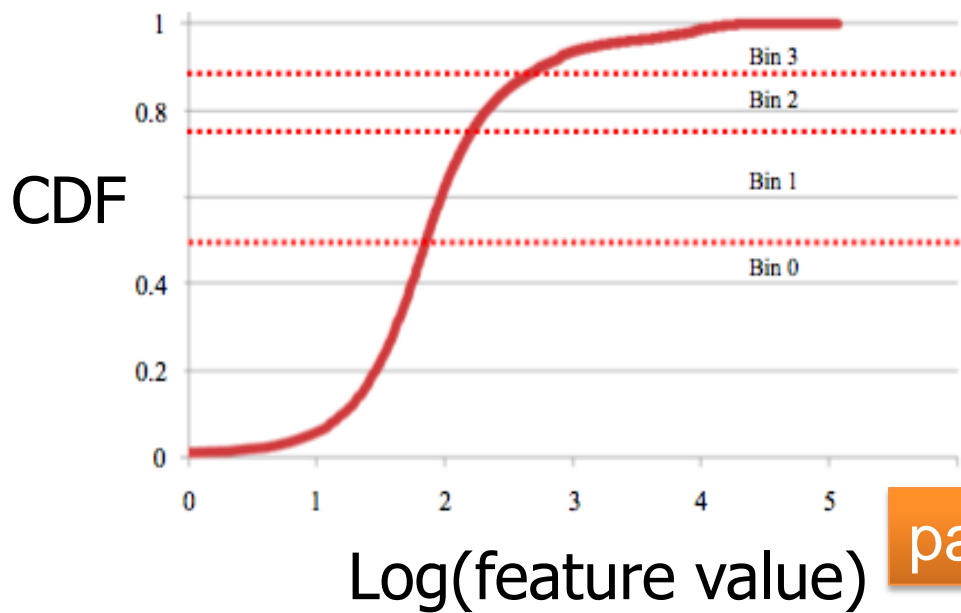


- **Regional** features
  - captures “kinds” of neighbors





# Computing recursive features



recursive features

vertical logarithmic binning of size  $p$

bin feature (integer)

not disagree at  $>s$  nodes

paired features ( $s$ -friend)

replace each CC in  $s$ -friend graph by single feature

retain simpler features

i.e. generated in fewer iterations

retained features from each iteration

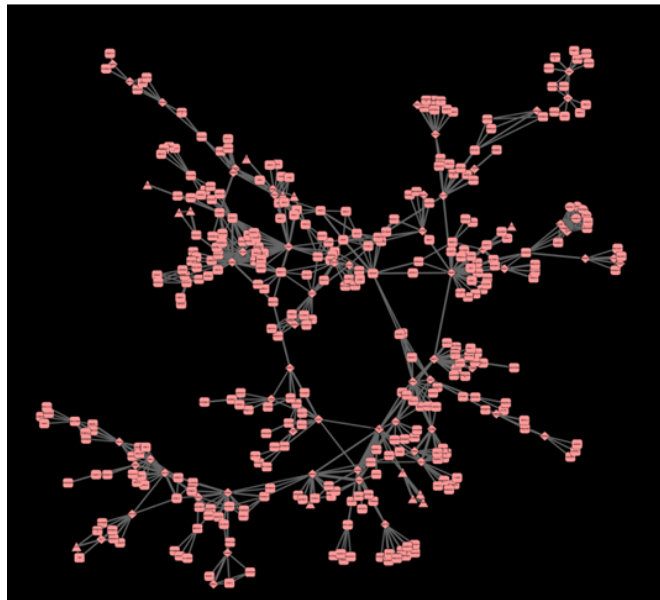
Prune highly correlated features

repeat until no pruning

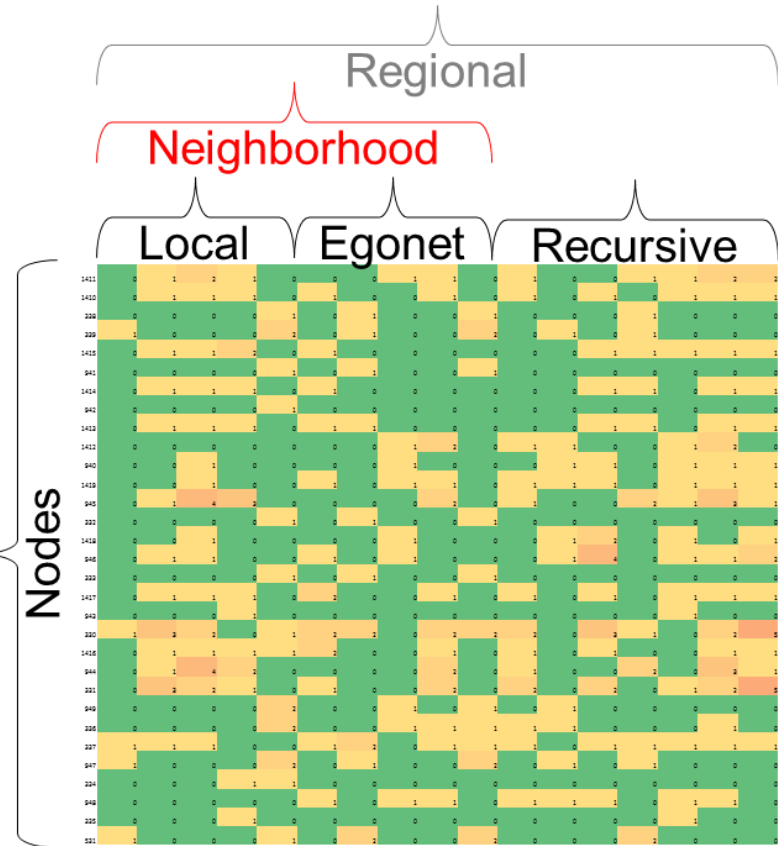
# Recursive structural features

- Capturing regional (**behavioral**) information in large graphs
- Feature construction **linear** in graph size
- Aggregates only for **numerical** features
- **Parameters**  $p$ ,  $s$  for binning and pruning

# ReFeX: Recursive Feature eXtraction



*ReFeX*



- Recursive features proved effective in **transfer learning, identity resolution** (yet to be studied for anomaly detection)

# Anomalies in Bipartite Graphs



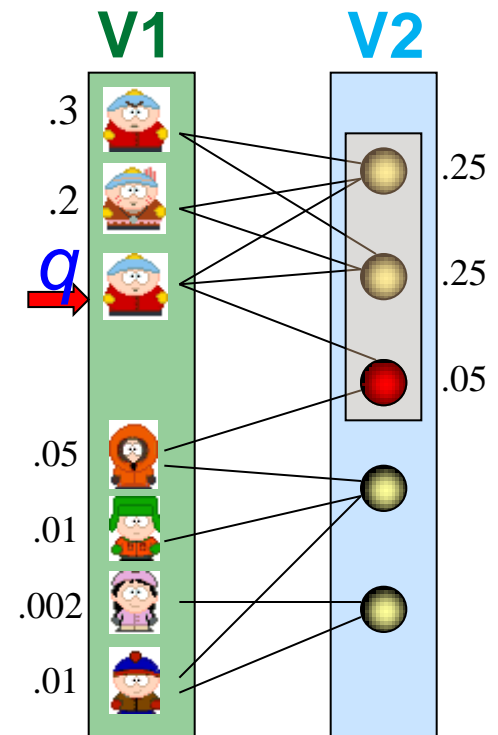
## ■ Problem:

### Q1. Neighborhood formation (NF)

- Given a query node  $q$  in  $V_1$ , what are the **relevance scores** of all the nodes in  $V_1$  to  $a$ ?

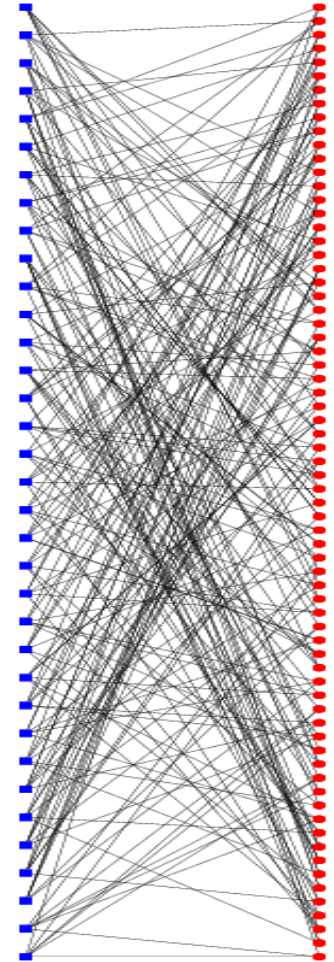
### Q2. Anomaly detection (AD)

- Given a query node  $q$  in  $V_1$ , what are the **normality scores** for nodes in  $V_2$  that link to  $a$ ?



# Applications of problem setting

- Publication network
  - (similar) authors vs. (unusual) papers
- P2P network
  - (similar) users vs. (“cross-border”) files
- Financial trading network
  - (similar) stocks vs. (cross-sector) traders
- Collaborative filtering
  - (similar) users vs. (“cross-border”) products



# 1) Neighborhood formation

## ■ Main idea:

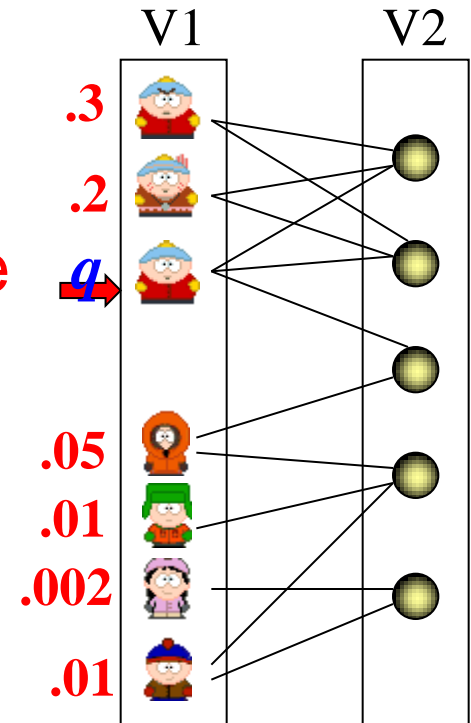
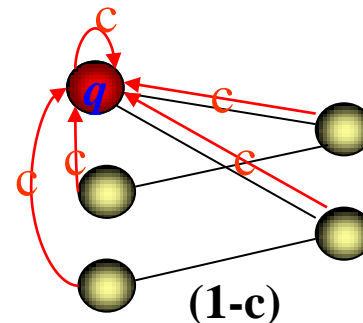
- Random-Walk-with Restart from  $q$
- Steady-state V1 prob.s as **relevance**

- (1) Construct transition matrix  $P$

$$P(a, b) = \begin{cases} \frac{1-c}{\text{outdeg}(a)} & \text{if } (a, b) \in E \\ 0 & \text{if } (a, b) \notin E \end{cases}$$

- (2) Fly-back prob.  $c$  to  $q$
- (3) Solve for steady state

$$\vec{u}_a^{(t+1)} = P \vec{u}_a^{(t)} + c\vec{q}$$



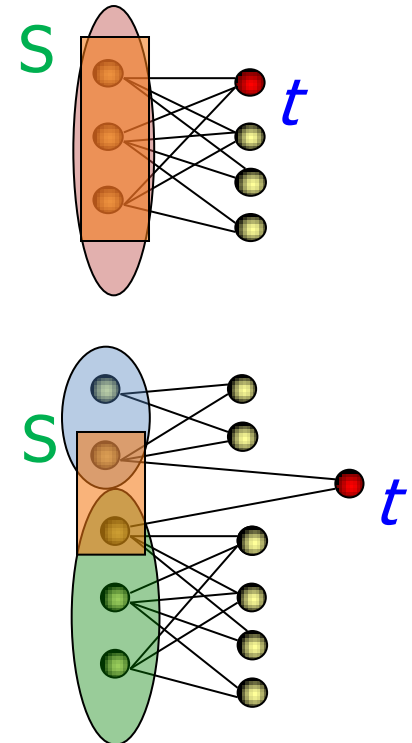
Approx: RWR on graph **partition** containing  $q$

## 2) Anomaly detection

- Main idea:

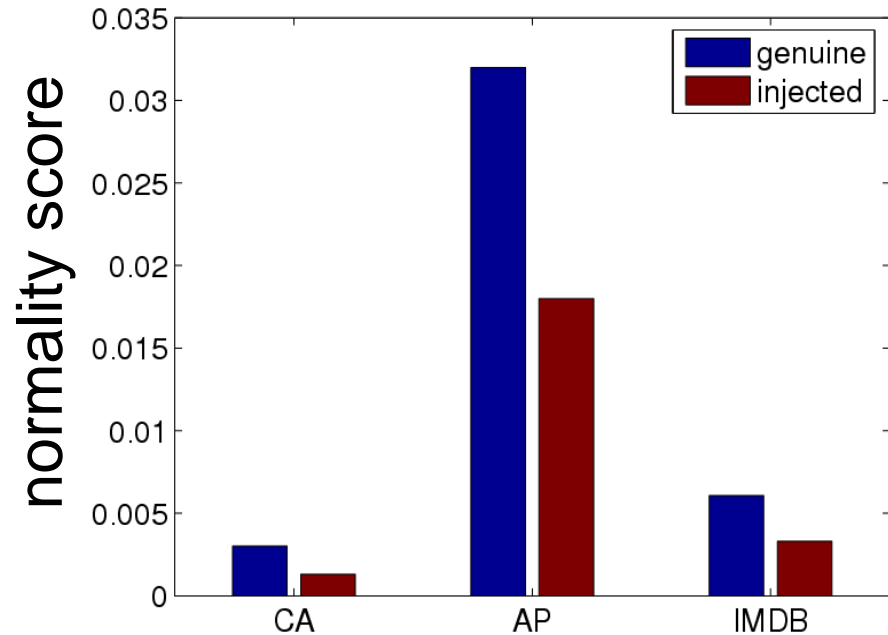
- Pairwise “normality” scores of neighbors( $t$ )
- Function of (e.g. avg) pair-wise scores

- (1) Find set  $S$  of nodes connected to  $t$
- (2) Compute  $|S| \times |S|$  normality matrix  $R$ 
  - asymmetric, diagonal reset to 0
- (3) Apply score function  $f(R)$ 
  - e.g.  $f(R) = \text{mean}(R)$



# Experiment

- 3 real datasets
  - DBLP conf-auth
  - DBLP auth-paper
  - IMDB movie-actor
- Randomly **inject** 100 nodes, each with  $k$  (avg. degree) edges (biased towards high-degree nodes)
- No qualitative results

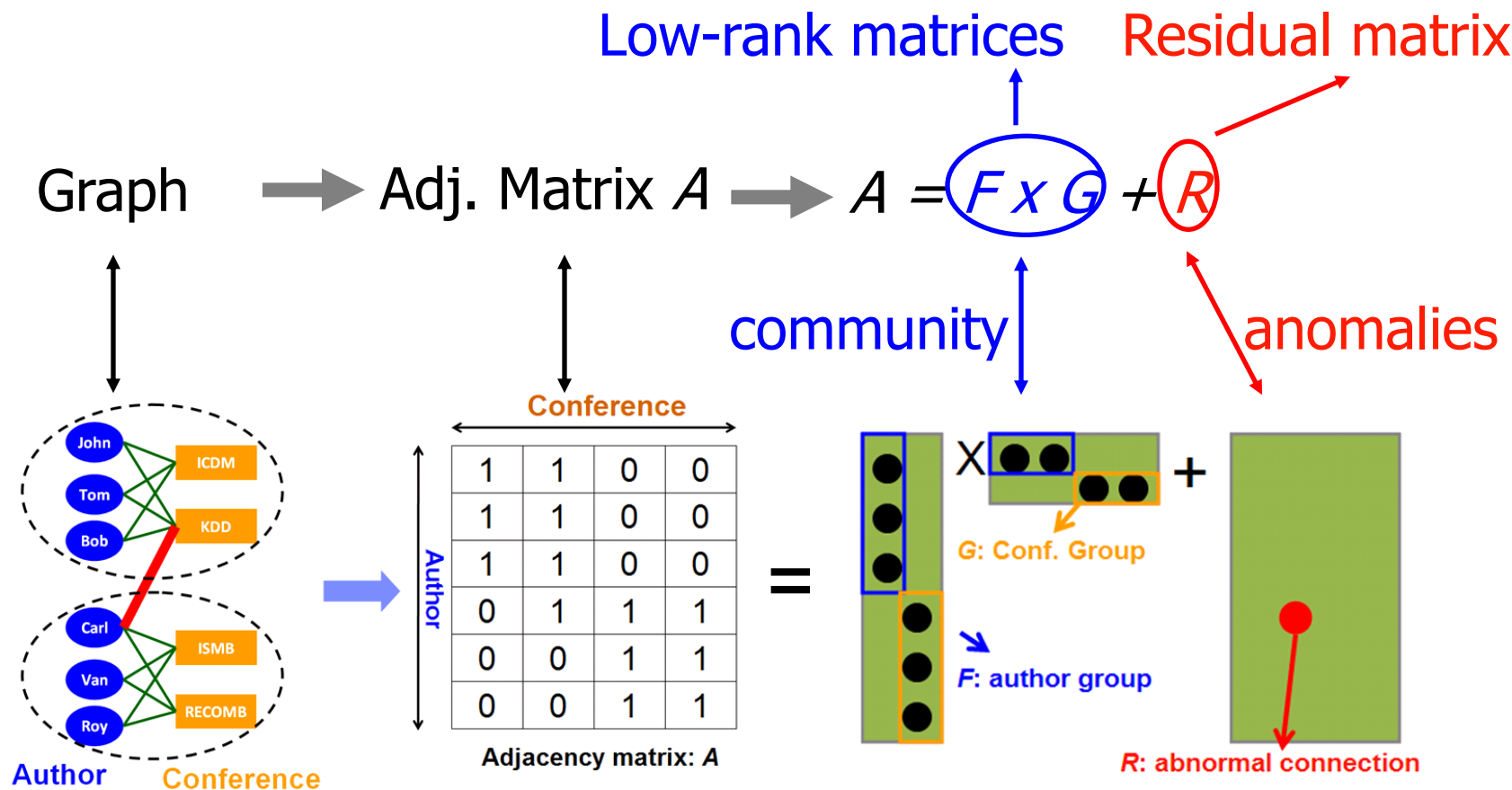




# Graph Anomalies by NNRMF



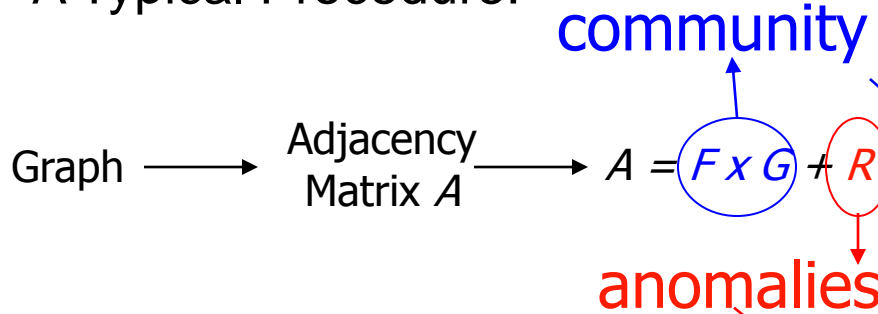
- Low-rank adjacency **matrix factorization** of a (sparse) graph reveals communities and anomalies



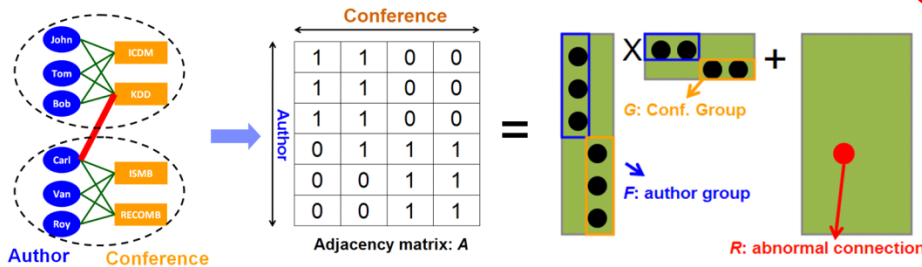
# Non-negativity constraints

- For improved interpretability

- A Typical Procedure:



- An Example



Interpretation by Non-negativity

**Non-negative Matrix Factorization**  
 $F \geq 0; G \geq 0$   
 (for community detection)

**Non-negative Residual Matrix Factorization**  
 $R(i,j) \geq 0; \text{ for } A(i,j) > 0$   
 (for anomaly detection)

# Optimization formulation

Common in  
Matrix Factorization

$\operatorname{argmin}_{\mathbf{F}, \mathbf{G}}$

$$\sum_{i,j, \mathbf{A}(i,j) > 0} (\mathbf{A}(i,j) - \mathbf{F}(i,:) \mathbf{G}(:,j))^2$$

s.t.

for all  $\mathbf{A}(i,j) > 0$  :

**Non-negative residual**

$$\mathbf{F}(i,:) \mathbf{G}(:,j) \leq \mathbf{A}(i,j)$$

- Q: How to find 'optimal'  $\mathbf{F}$  and  $\mathbf{G}$ ?
  - D1: Quality  $\leftrightarrow$  C1: objective non-convex
  - D2: Scalability  $\leftrightarrow$  C2: large graph size

# Optimization: batch

## ■ Basic Idea 1: Alternating

$$\operatorname{argmin}_{\mathbf{F}, \mathbf{G}} \sum (\mathbf{A}(i, j) - \mathbf{F}(i, :) \mathbf{G}(:, j))^2$$

Not convex w.r.t.  $F$  and  $G$ , jointly

But convex if fixing either  $F$  or  $G$

## ■ Basic Idea 2: Separation

$$\operatorname{argmin}_{\mathbf{G}} \sum_{i, j, \mathbf{A}(i, j) > 0} (\mathbf{A}(i, j) - \mathbf{F}(i, :) \mathbf{G}(:, j))^2 \quad \operatorname{argmin}_{\mathbf{G}} \sum_{i, j, \mathbf{A}(i, j) > 0} (\mathbf{A}(i, j) - \mathbf{F}(i, :) \mathbf{G}(:, j))^2$$

**s.t.** for all  $\mathbf{A}(i, j) > 0$  :  $\mathbf{F}(i, :) \mathbf{G}(:, j) \leq \mathbf{A}(i, j)$       **s.t.** for all  $\mathbf{A}(i, j) > 0$  :  $\mathbf{F}(i, :) \mathbf{G}(:, j) \leq \mathbf{A}(i, j)$



Standard Quadratic Programming

## Overall Complexity: Polynomial



# Optimization: incremental

- Basic Idea 0: Recursive
- Basic Idea 1: Alternating

$$\operatorname{argmin}_{f,g} \sum_{i,j, A(i,j)>0} (A(i,j) - f(i)g(j))^2$$

For each  $j$

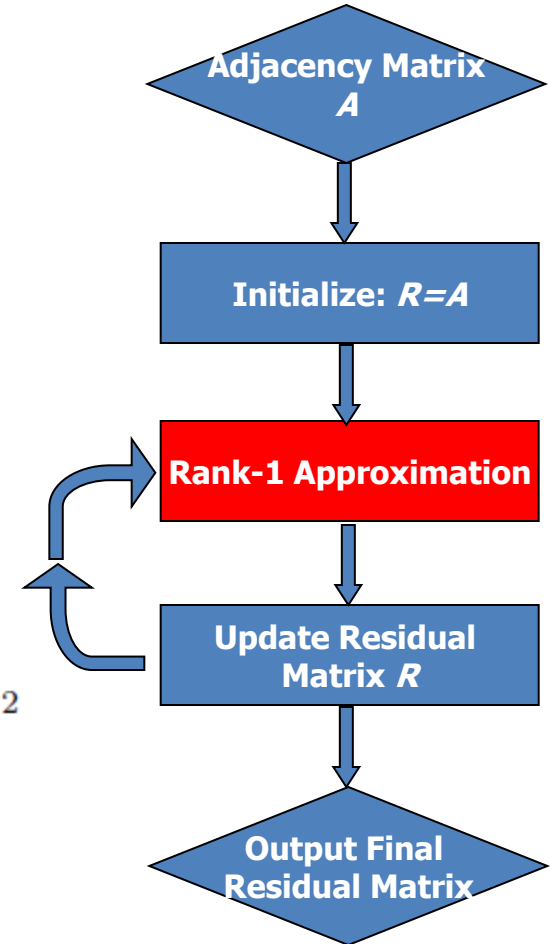
- Basic Idea 2: Separation

QP for a single variable  
w/ boundary constrains

$$\operatorname{argmin}_{g_j} \sum_{i, A(i,j)>0} (A(i,j) - f(i)g(j))^2$$

s.t. for all  $A(i,j) > 0$  :  
 $f(i)g(j) \leq A(i,j)$

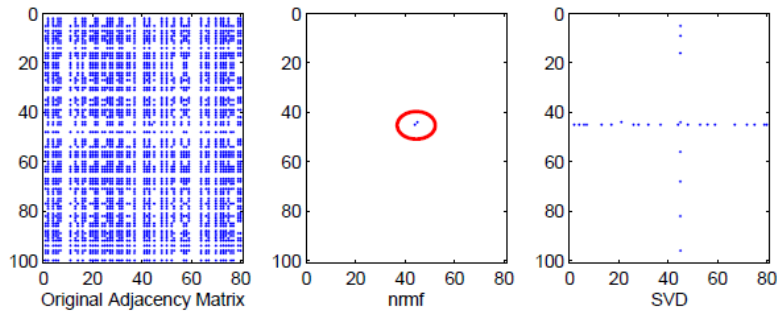
Solved in  
constant time



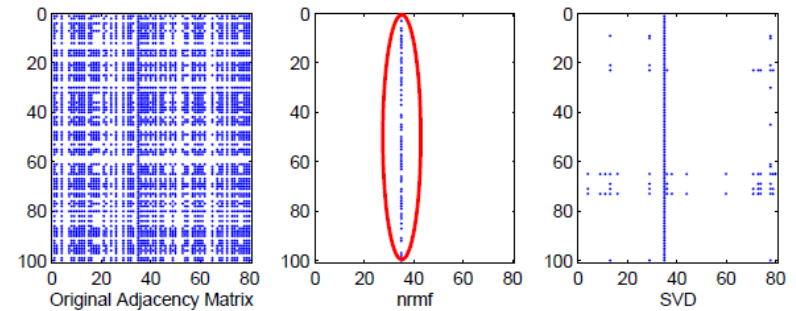
Overall Complexity: Linear wrt # of edges

# Experiments

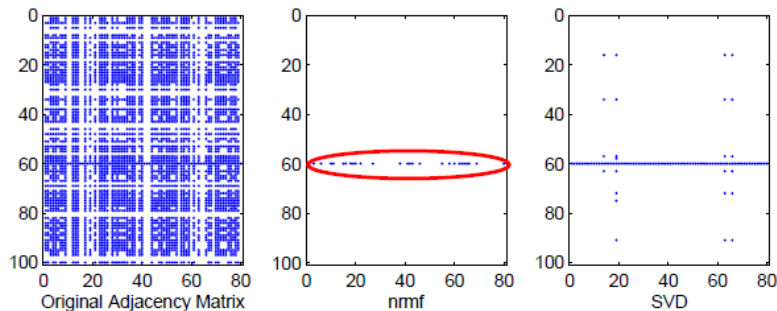
- NNrMF can spot 4 types of anomalies



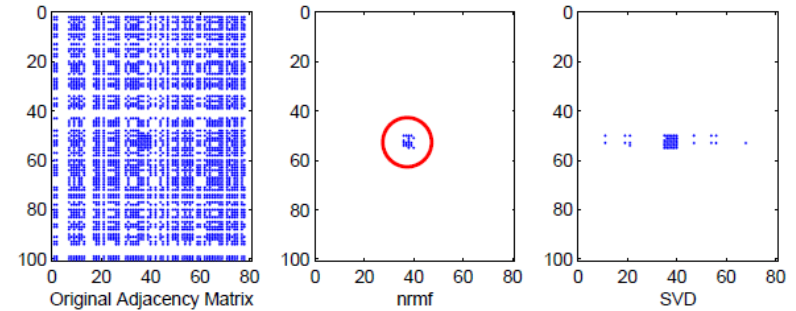
(a) strange connection



(b) port scanning



(c) ddos



(d) bipartite core

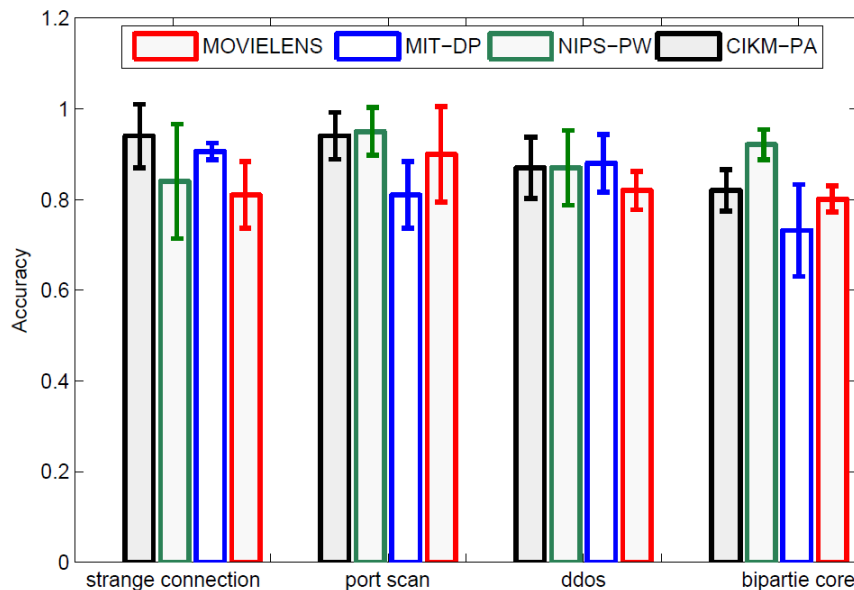
NNrMF residuals  $\uparrow$  SVD residuals  $\uparrow$   
residuals residuals (top-k edges)

# Experiments

- 4 real datasets, with injected anomalies

## Effectiveness

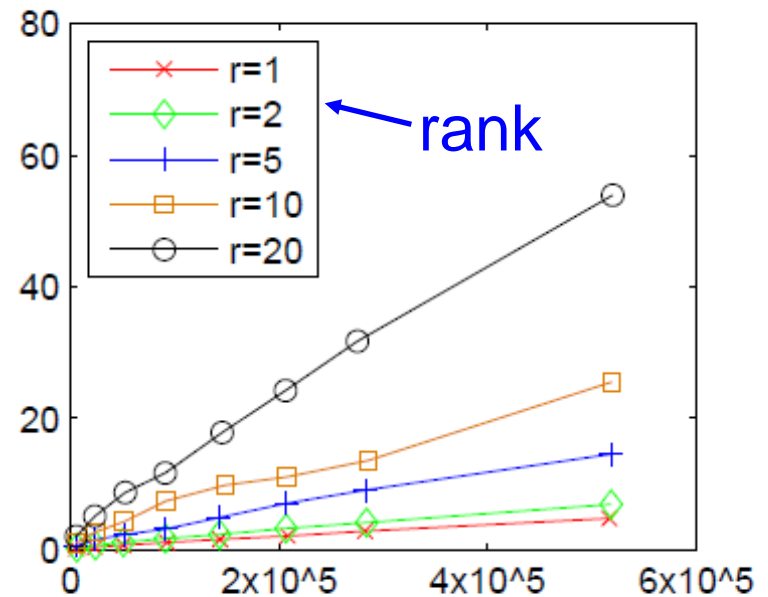
### Accuracy



### Anomaly Type

## Efficiency

### Wall-clock Time



### # of edges

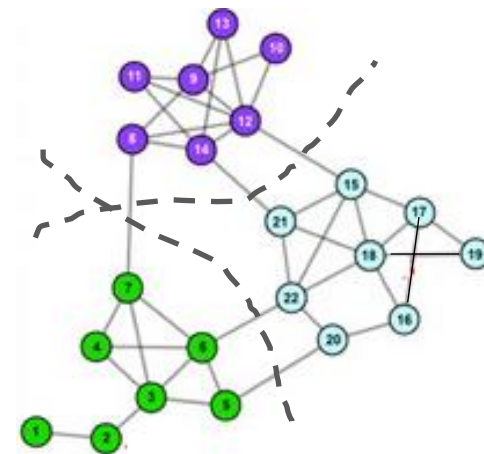
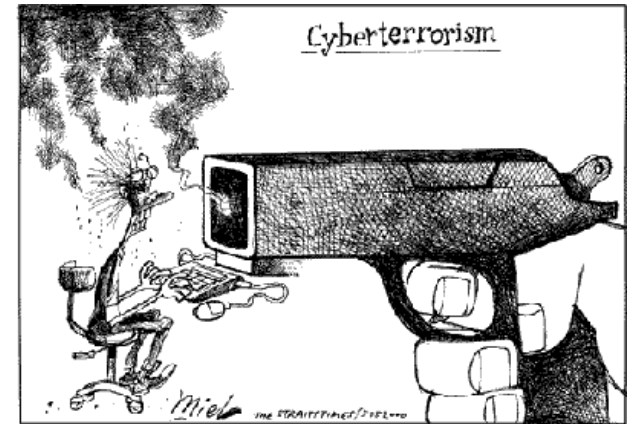
# Intrusion as (Anti)social Communication

## ■ Problem:

Q. How to detect **malicious** attacks in computer networks?

## ■ Main insight for intrusion:

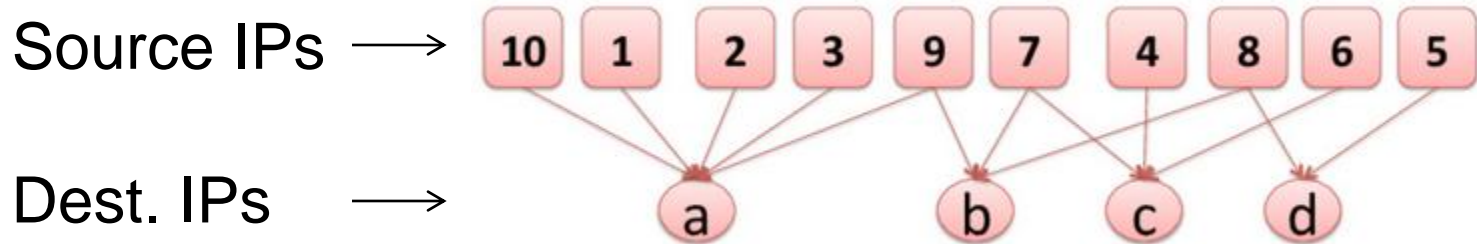
- ❑ entering a community to which one doesn't belong
- ❑ look for communication that does not respect **community boundaries**



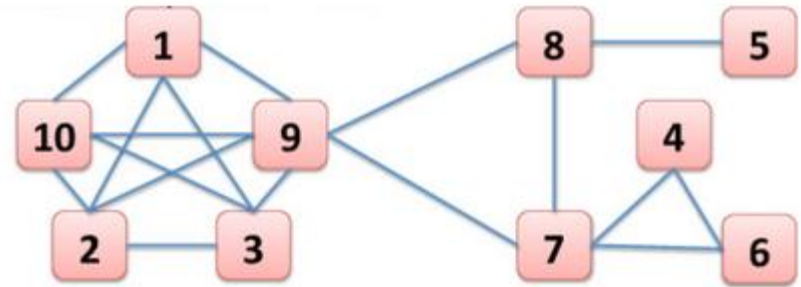


# Problem formulation

- Network representation as a **bipartite graph**



- Source and destination IPs may overlap
- One mode projection  $G_P$ : connect two source IPs with at least 1 common neighbor
- Alternative  $G_w$ : weigh by correlation coefficient



# Intrusion data with ground truth

- Data: netflow traffic
  - from a large European ISP
  - 2 weeks data in 2007: source IP, dest IP, start/end time, number of bytes/packets sent
  - **Ground truth**: traffic sources that attempted an intrusion as recorded by **Dshield**
    - **known IPs** sending malicious or unwanted traffic



\* <http://www.dshield.org/>

# Detection methods

- **Community detection:** Standard community detection methods fail to distinguish **known IPs** from communities

Size of Cluster	# of Clusters	# of DShields
6784	1	158
986	1	1
8 to 243	10	0
$\leq 7$	56	2
Total	68	161

- **Cut-vertices:**

Iteratively remove cut-vertices

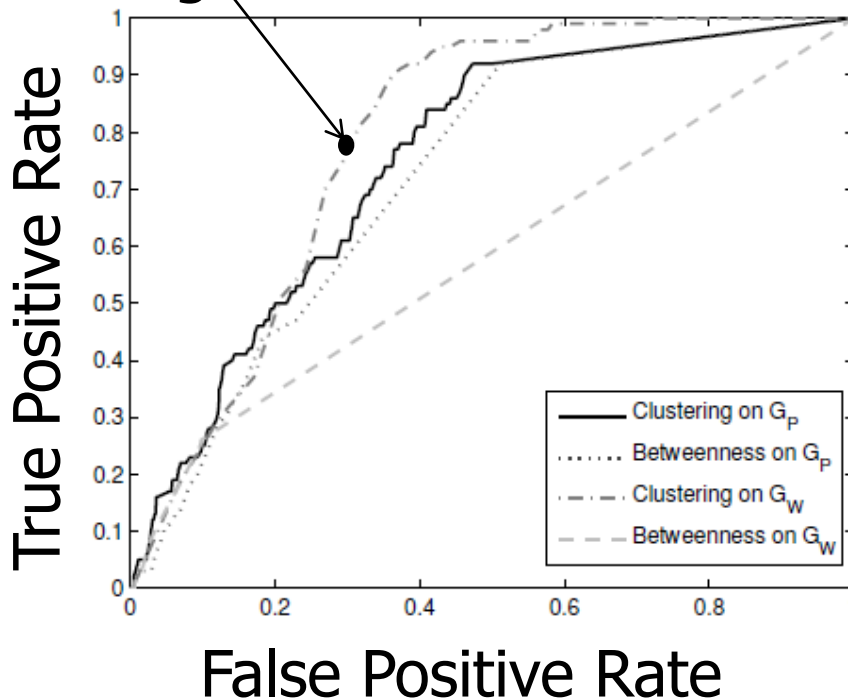
- 6.6% of cut-vertices are Dshields (randomization yields significance; (1-2.2%) at 0.05)

→ **Clustering and betweenness** deemed discriminative

# Experiments

- **Malicious** if clustering/betweenness below/above threshold

for a given threshold



	Mean(AUC)	SE(AUC)
Clustering on $G_P$	0.7440	0.0103
Betweenness on $G_P$	0.7180	0.0084
Clustering on $G_W$	0.7625	0.0080
Betweenness on $G_W$	0.5621	0.0034

- **Clustering** gives better discrimination
- $G_W$  does not provide much improvement over  $G_P$

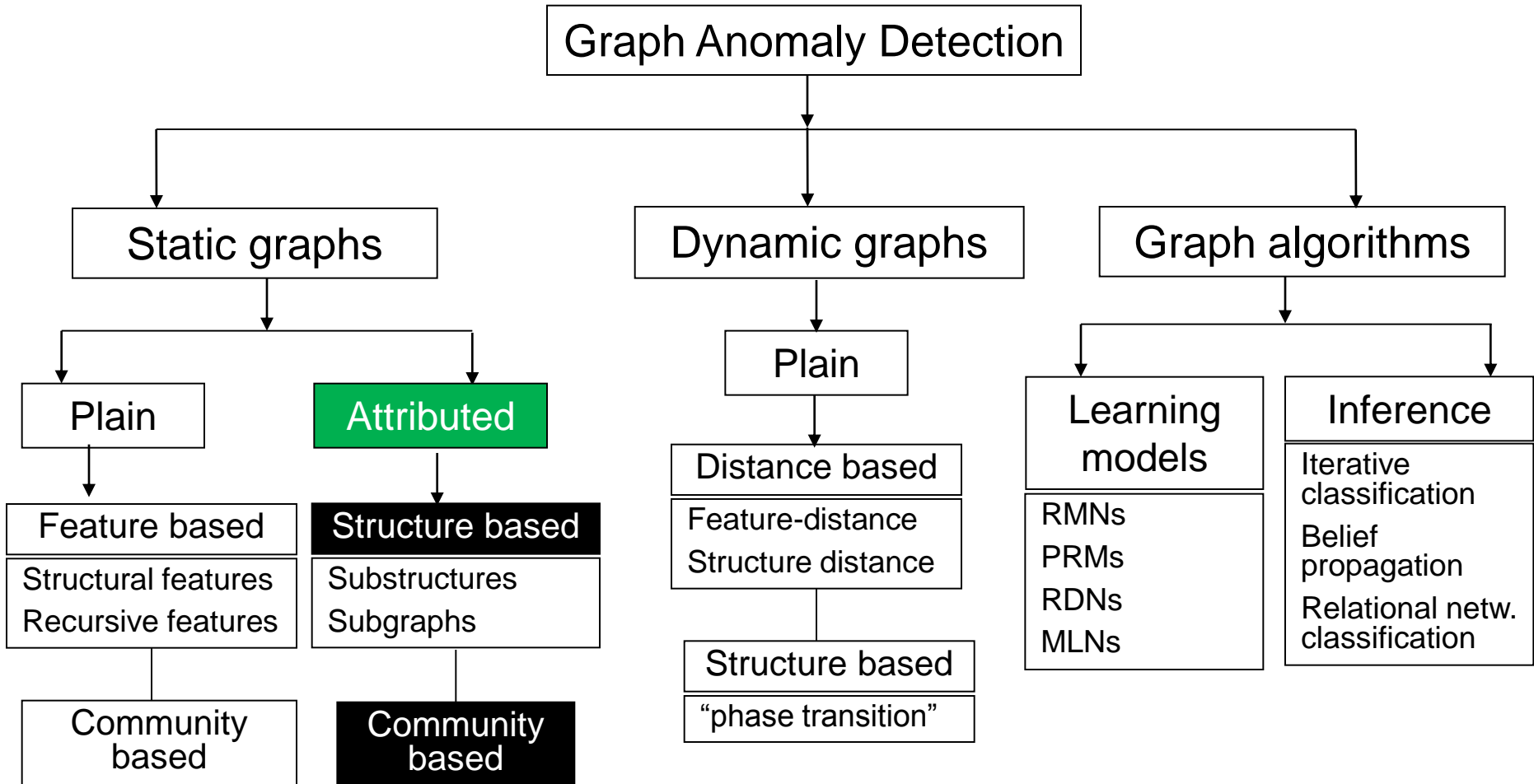
# Part I: References (plain graphs)

- L. Akoglu, M. McGlohon, C. Faloutsos. [OddBall: Spotting Anomalies in Weighted Graphs](#). PAKDD, 2010.
- K. Henderson, B. Gallagher, L. Li, L. Akoglu, T. Eliassi-Rad, H. Tong, C. Faloutsos. [It's Who You Know: Graph Mining Using Recursive Structural Features](#). KDD, 2011.
- J. Sun, H. Qu, D. Chakrabarti, and C. Faloutsos. [Neighborhood formation and anomaly detection in bipartite graphs](#). ICDM, 2005.
- Hanghang Tong, Ching-Yung Lin: [Non-Negative Residual Matrix Factorization with Application to Graph Anomaly Detection](#). SDM, pages 143-153, 2011.
- Q. Ding, N. Katenka, P. Barford, E. Kolaczyk, and M. Crovella. [Intrusion as \(Anti\)social Communication: Characterization and Detection](#). KDD, 2012.

# Part I: Outline

- Overview: Outliers in **clouds of points**
  - Outliers in **numerical** data points
    - distance-based, density-based, ...
  - Outliers in **categorical** data points
    - model-based
- Anomaly detection in **graph data**
  - Anomalies in unlabeled, **plain** graphs
  - ➔ Anomalies in node-/edge-labeled, **attributed** graphs

# Taxonomy

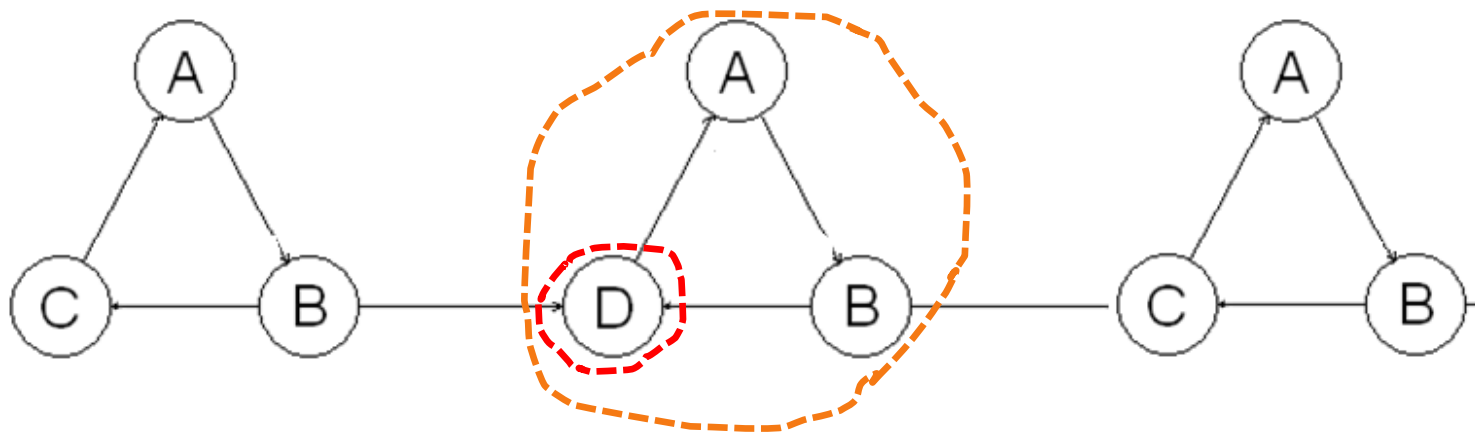


# Anomalies in labeled graphs

## ■ Problem:

Q1. Given a graph in which nodes and edges contain (non-unique) labels, what are unusual substructures?

Q2. Given a set of subgraphs, what are the unusual subgraphs?



**Note:** assumption is anomalies are connected



# Background

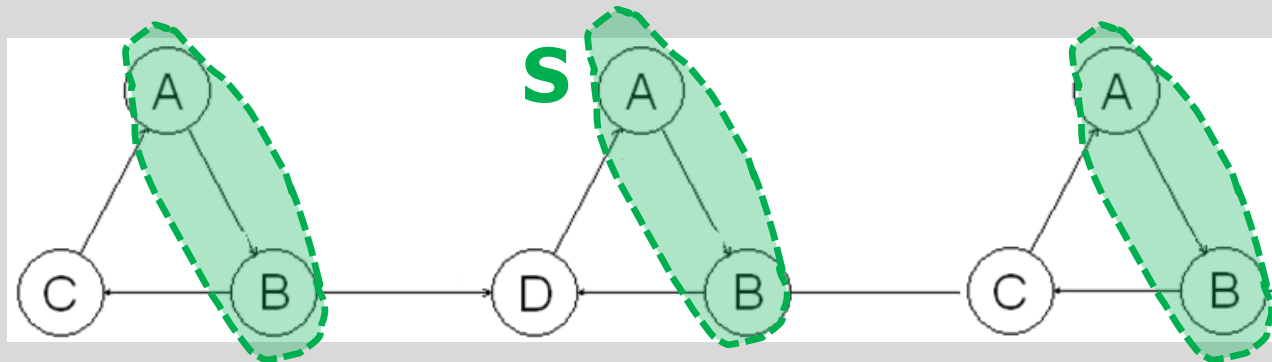
- **Subdue**\*: An algorithm for detecting repetitive patterns (substructures) within graphs.
- **Substructure**: A connected subgraph of the overall graph.
- **Compressing** a graph: Replacing each instance of the substructure with a new vertex representing that substructure.
- **Description Length (DL)**: Number of bits needed to encode a piece of data

\* <http://ailab.wsu.edu/subdue/>

# Background

- **Subdue** uses the following heuristic:
  - The best substructure is the one that **minimizes**

$$F1(S,G) = DL(G | S) + DL(S)$$
    - G: Entire graph, S: The substructure,
    - $DL(G|S)$  is the DL of G after compressing it using S,
    - $DL(S)$  is the description length of the substructure.



- Iterations after **compressing** at each step

# Background

Given **database D** and set of models for **D**, **Minimum Description Length** selects **model M** that minimizes

$$\underbrace{L(M)} + \underbrace{L(D|M)}$$

length in bits: **model M**      length in bits: **data, description of encoded by M**



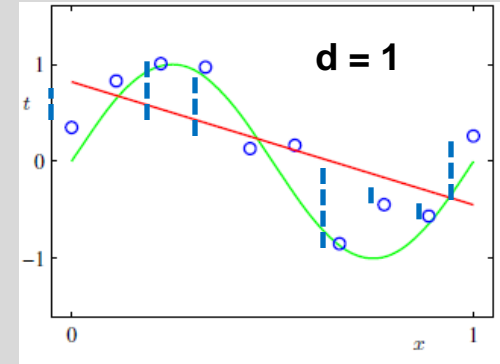
$$a_1x + a_0$$



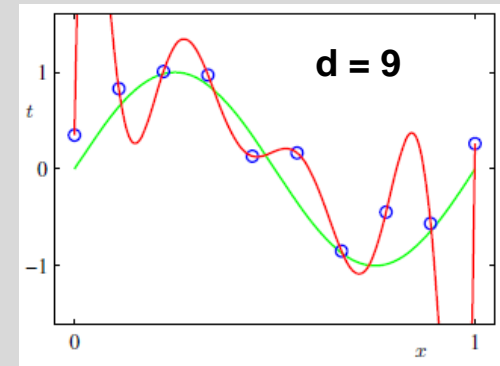
deltas

VS.

$$a_9x^9 + \dots + a_1x + a_0 \quad \{ \}$$



VS.



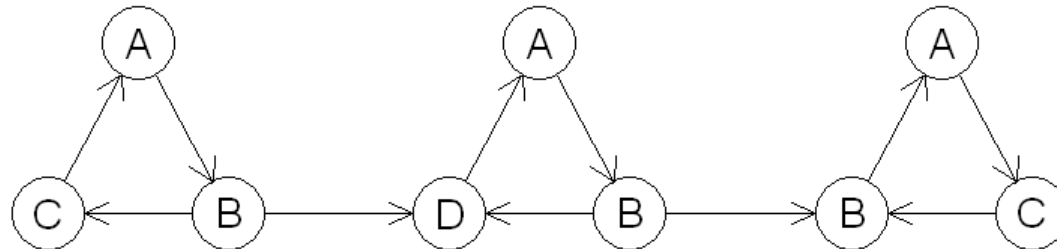
Bishop: PR&ML

# 1) Anomalous Substructures

- Main idea: **anomalies** (by def.) occur infrequently, they are roughly **opposite to “best substructures”**
  - Find substructures **S** that maximize **F1(S,G)**?
    - **Nope**, it flags all single nodes as anomalies!
  - Instead, find those that **minimize**  
**F2(S, G) = Size(S) \* Instances(S,G)**
    - Approximate inverse of **F1(S,G)**
- **Intuition:** Larger substructures are expected to occur few times; the smaller the substructure, the less likely it is rare

# Example

- **$F2(S, G) = \text{Size}(S) * \text{Instances}(S, G)$** 
  - For node D,  $F2 = 1 * 1 = 1$
  - For  $A \rightarrow C$  and  $D \rightarrow A$ , it is  $2 * 1 = 2$
  - For G (whole graph), it is  $9 * 1 = 9$
- Hence D is considered the most anomalous.



- **Note:** Usually a threshold for **F2** is used and anomalies are ranked by their scores.

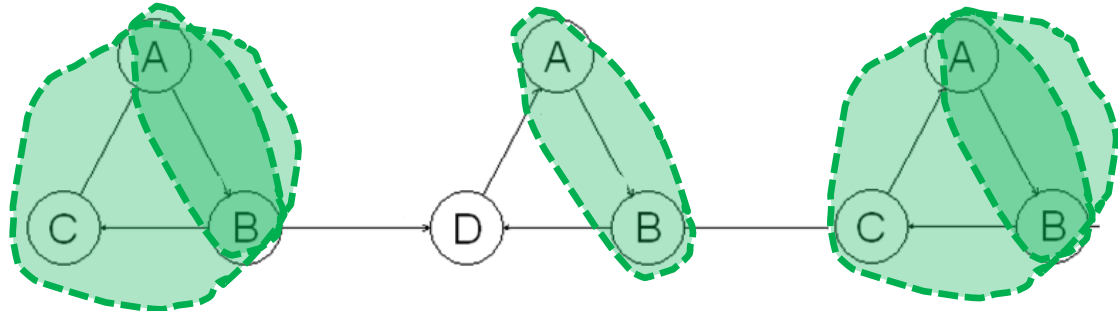
## 2) Anomalous Subgraphs

- Main idea: subgraphs containing **few common substructures** are generally more **anomalous**
  - Define compressibility score  $A$  in  $[0,1]$

$$A = 1 - \frac{1}{n} \sum_{i=1}^n (n - i + 1) * c_i$$

# Subdue iterations →  $n$ 
fast drop off in early iterations →  $(n - i + 1)$ 
fraction compressed at  $i$ th iteration →  $c_i$

$$\frac{DL_{i-1}(G) - DL_i(G)}{DL_0(G)}$$

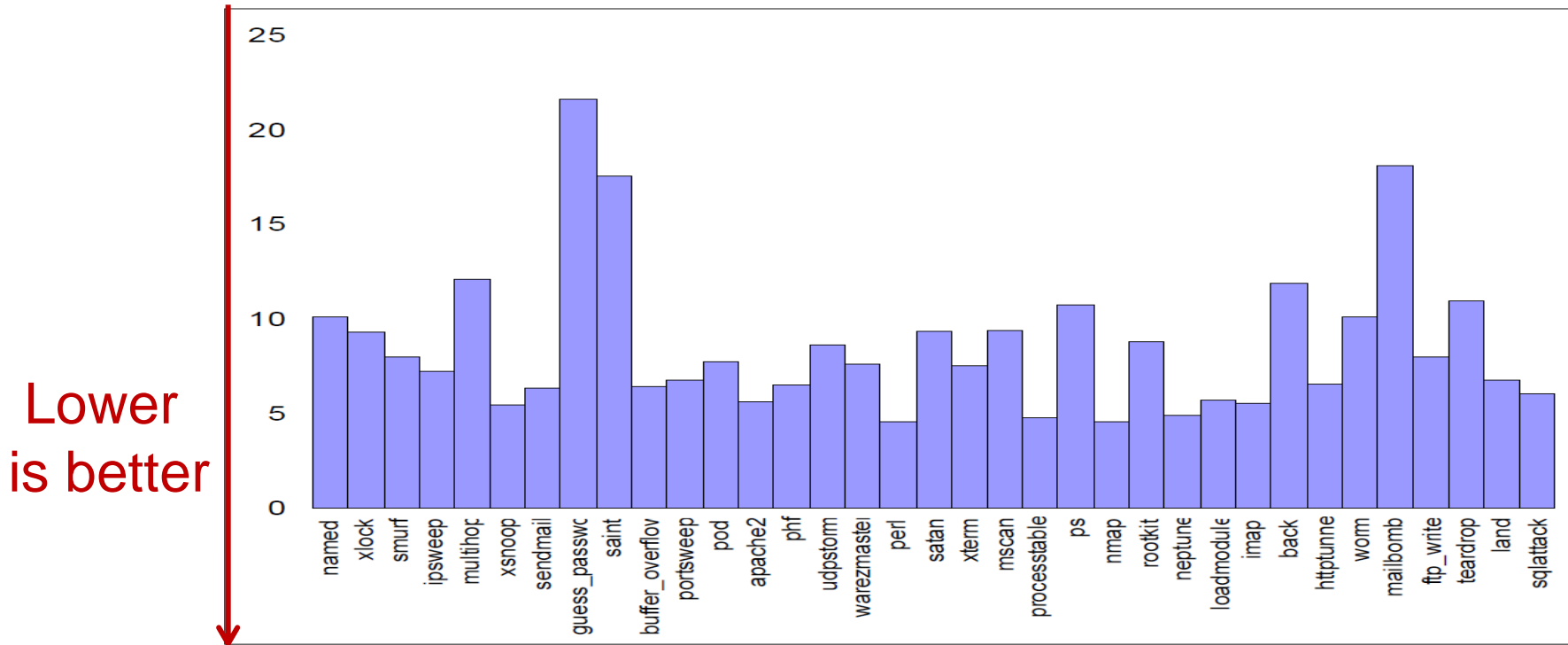


# Experiments



- **Data:** 1999 KDD Cup Network Intrusion
  - **Ground truth:** connection records, “normal” or attack (37 types), 41 features of connection (duration, protocol type, number of bytes, etc.)
  - Each individual test involved **50 records** of which **only one is of a particular attack type.**
- Use Subdue to find anomalous substructures
  - Prune all subgraphs with  $\text{size} > 3$ ,  $F2 > 6$  (arbitrary)

# Performance



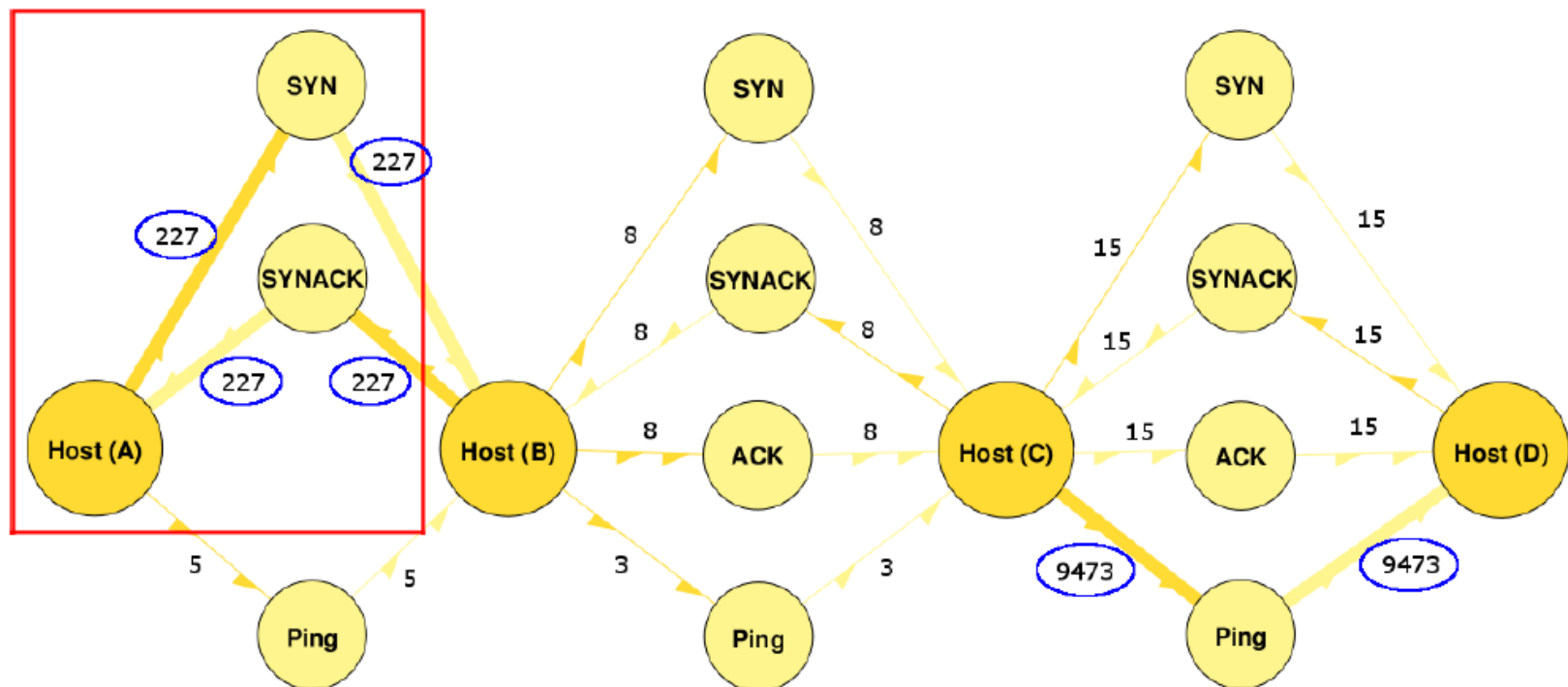
- **Note:** Degree of anomaly  $D(S)$ :  $1/F2$ 
  - Attack accounts for  $D(S1) / (\text{Sum } [D(Si)])$
  - e.g., if  $F2 = (2, 3, 4)$  for  $(S1, S2, S3)$  and  $S2$  occurs in the attack, then attack accounts for  $(1/3) / (1/2 + 1/3 + 1/4) = 4/13$  of discovered anomalies



# Anomalies with numeric labels

- How about **numeric** labels?
  - Noble & Cook work with **categorical** labels

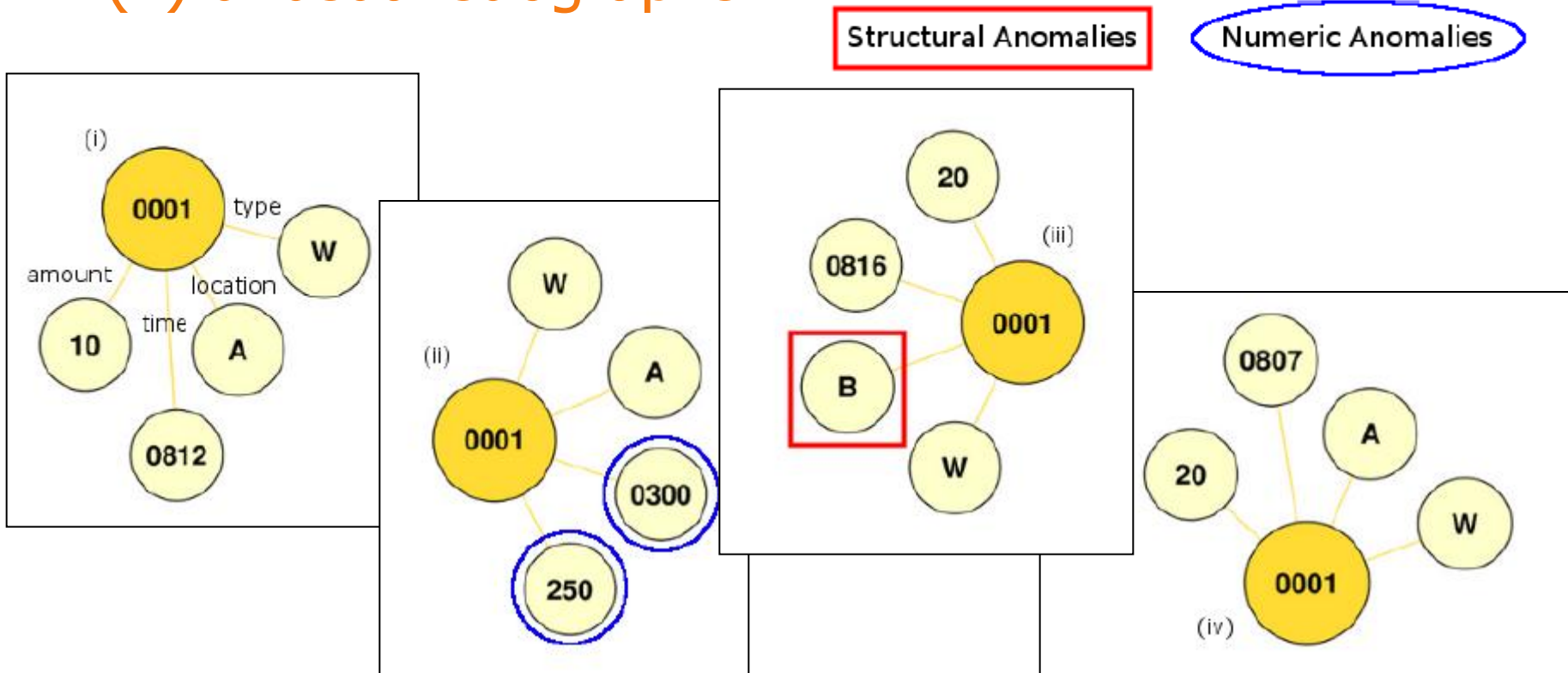
## (1) unusual substructures



# Anomalies with numeric labels

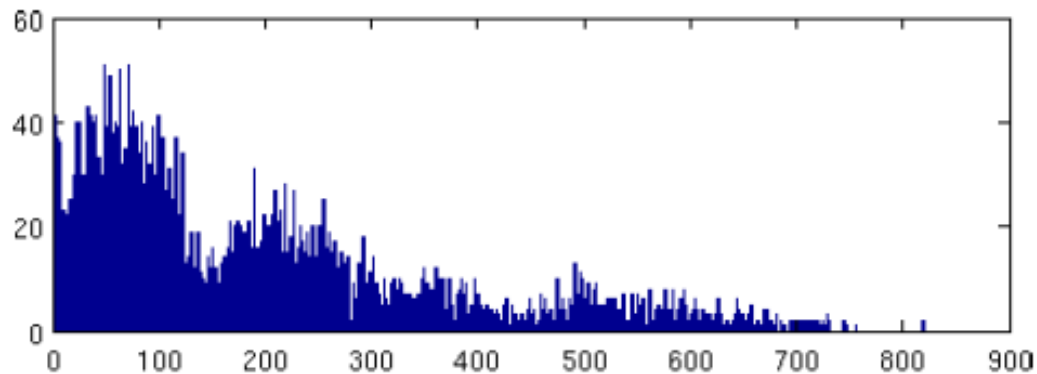
- How about **numeric** labels?
  - Noble & Cook work with **categorical** labels

## (2) unusual subgraphs



# Anomalies with numeric labels

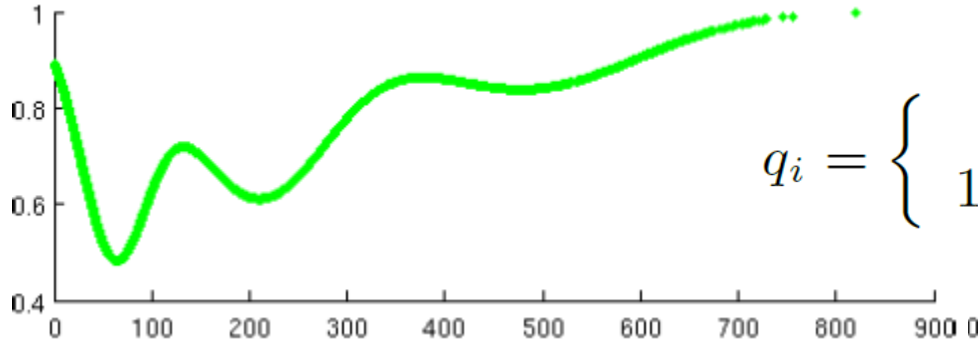
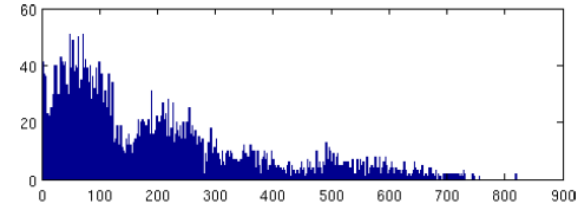
- Main idea (discretization):
  - assign categoric label  $q_0$  to “normal” values, and
  - “outlierness” score  $q_i$  to all others  $i$
- Example: empirical distribution of a label



- Several “outlierness” scores (pdf-fitting, kNN, LOF, clustering-based)

# Discretization

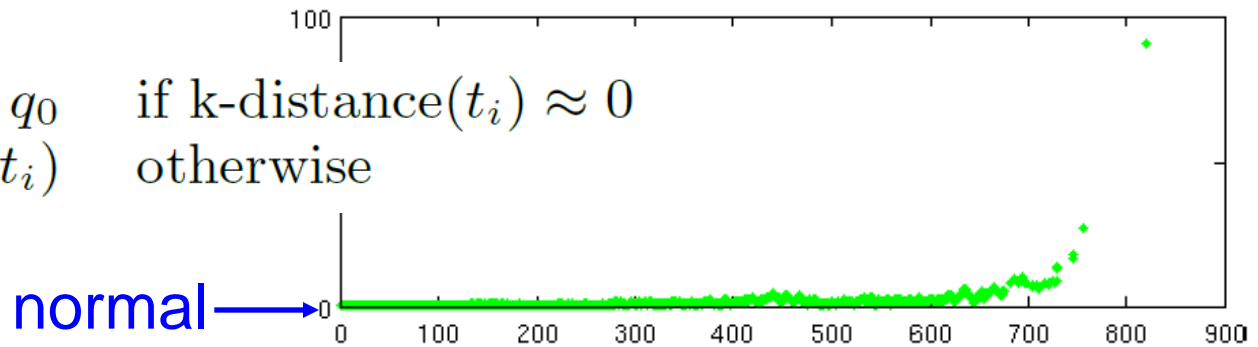
## Model fitting (GMM)



$$q_i = \begin{cases} q_0 & \text{if } 1 - P(t_i) < q_a \\ 1 - P(t_i) & \text{otherwise} \end{cases}$$

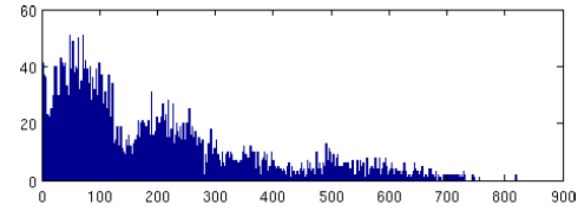
## kNN distance

$$q_i = \begin{cases} q_0 & \text{if k-distance}(t_i) \approx 0 \\ \text{k-distance}(t_i) & \text{otherwise} \end{cases}$$



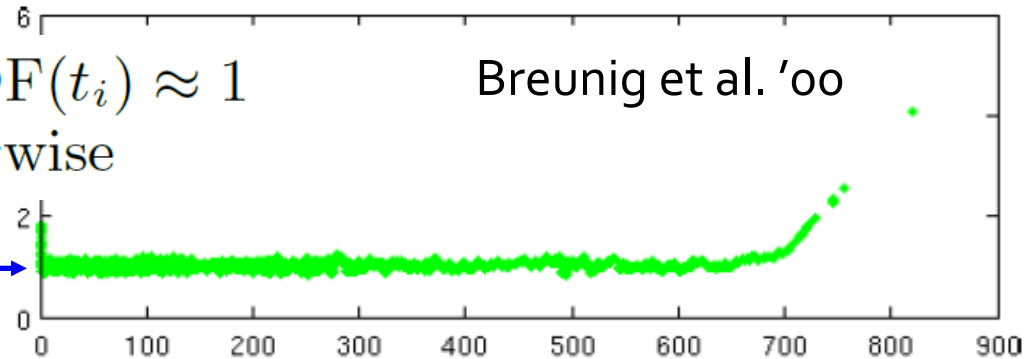
# Discretization

## Density outlier score (LOF)

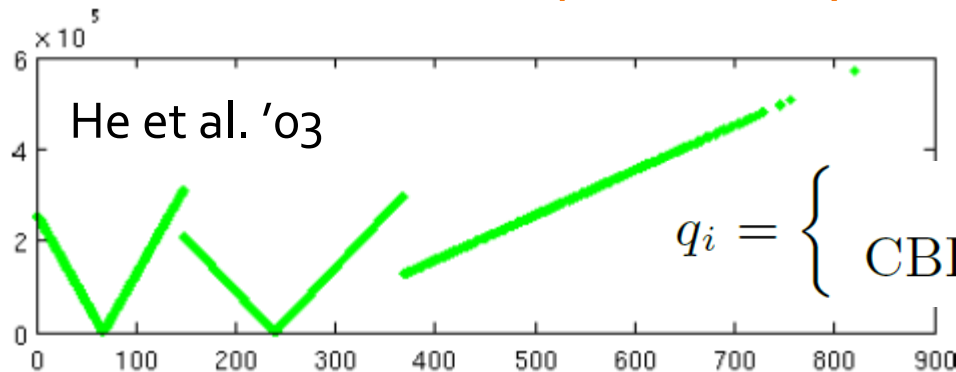


$$q_i = \begin{cases} q_0 & \text{if } \text{LOF}(t_i) \approx 1 \\ \text{LOF}(t_i) & \text{otherwise} \end{cases}$$

normal →



## Cluster-based (CbLOF)



$$q_i = \begin{cases} q_0 & \text{if } \text{CbLOF}(t_i) < q_a \\ \text{CbLOF}(t_i) & \text{otherwise} \end{cases}$$

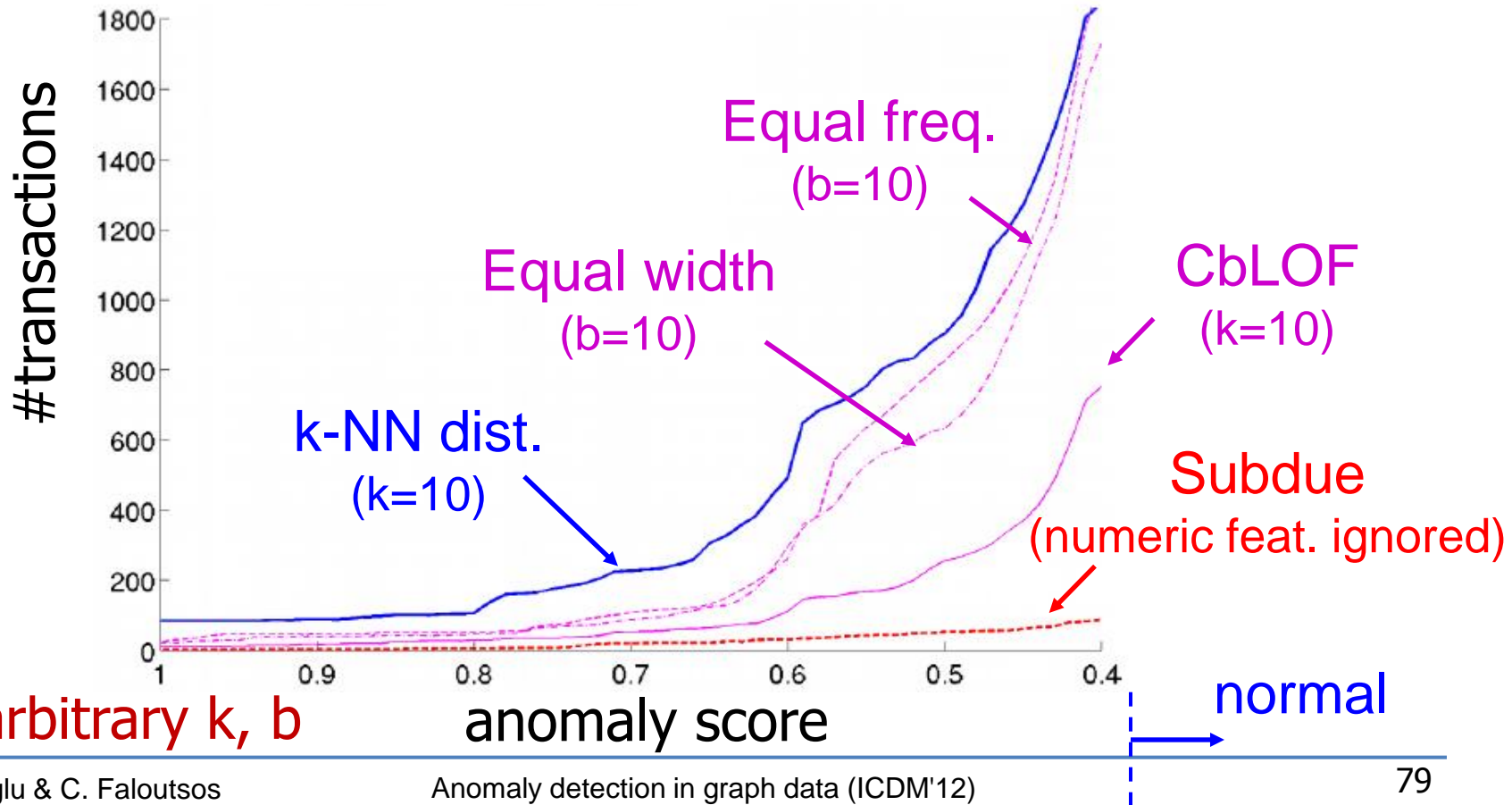
distance to closest "large" (k-means) cluster centroid

# Discretization

- Other possible discretization techniques
  - SAX (**S**ymbolic **A**ggregate appro**X**imation)
    - <http://www.cs.ucr.edu/~eamonn/SAX.htm>
  - MDL-binning
    - P. Kontkanen and P. Myllymäki. *MDL histogram density estimation*. In AISTAT, 2007.
  - Minimum entropy discretization
    - U.M. Fayyad and K.B. Irani. *Multi-interval discretization of continuous-valued attributes for classification learning*. In Proc. IJCAI, pages 800–805, 1989.
  - Logarithmic binning
    - especially for skewed distributions

# Experiment

- **Data:** Access card transaction graphs
  - node: door sensor, edge  $(u,w)$ : movement  $u \rightarrow w$ , weight $(u,w)$ : time  $u \rightarrow w$  (only numeric attribute)



# Anomalies in labeled graphs

## ■ Problem:

Q1. **Given** a graph in which nodes and edges contain **(non-unique) labels**, how to **find** substructures that are **very similar to, though not the same as, a normative substructure?** (“best substructure” as for Subdue)\*

## ■ Intuition:

*“The more successful money-laundering apparatus is in imitating the patterns and behavior of legitimate transactions, the less the likelihood of it being exposed.”*

– *United Nations Office on Drugs and Crime*





# Formal definition

- Given graph  $G$  with a normative substructure  $S$ , a substructure  $S'$  is anomalous if difference  $d$  between  $S$  and  $S'$  satisfies  $0 < d \leq X$ , where  $X$  is a (user-defined) threshold and  $d$  is a measure of the unexpected structural difference.
- Assumptions
  - Majority of  $G$  consists of a normative pattern, and no more than  $X\%$  of it is altered in an anomaly.
  - Anomalies consist of **one or more modifications, insertions or deletions.**
  - Normative pattern is connected.

# Three Types of Anomalies

- 1) **GBAD-MDL** (Minimum Descriptive Length):  
anomalous **modifications**
- 2) **GBAD-P** (Probability): anomalous **insertions**
- 3) **GBAD-MPS** (Maximum Partial Substructure):  
anomalous **deletions**

**Note:** prone to miss more than one type of anomaly

- e.g., a deletion followed by modification

# 1) Information Theoretic Approach

- Find normative substructure **S** that minimizes

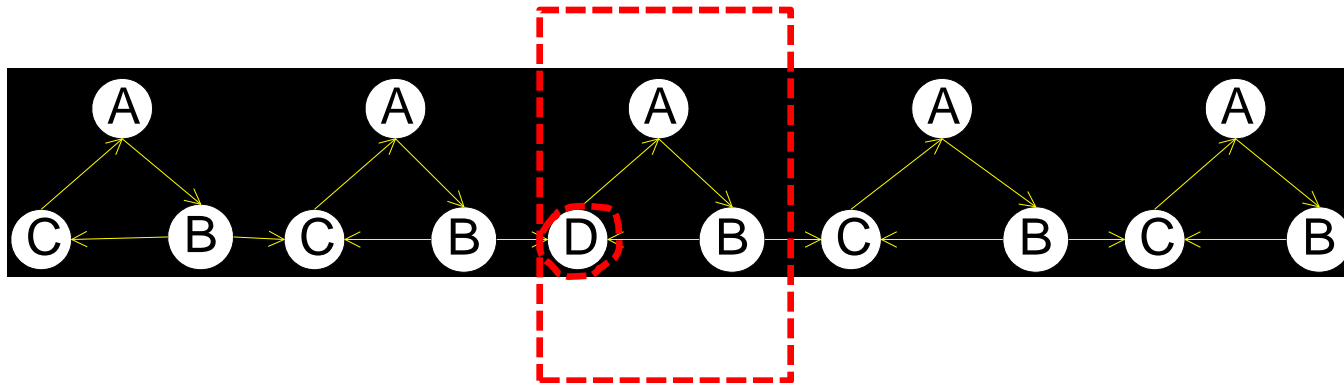
$$F(\mathbf{S}, \mathbf{G}) = DL(\mathbf{G} | \mathbf{S}) + DL(\mathbf{S})$$

- For each instance  $I_k$  of **S**

$$\text{anomalyScore}(I_k) = \text{freq}(I_k) * \text{matchcost}(I_k, S)$$

cost to modify  $I_k$  into S

- Example:

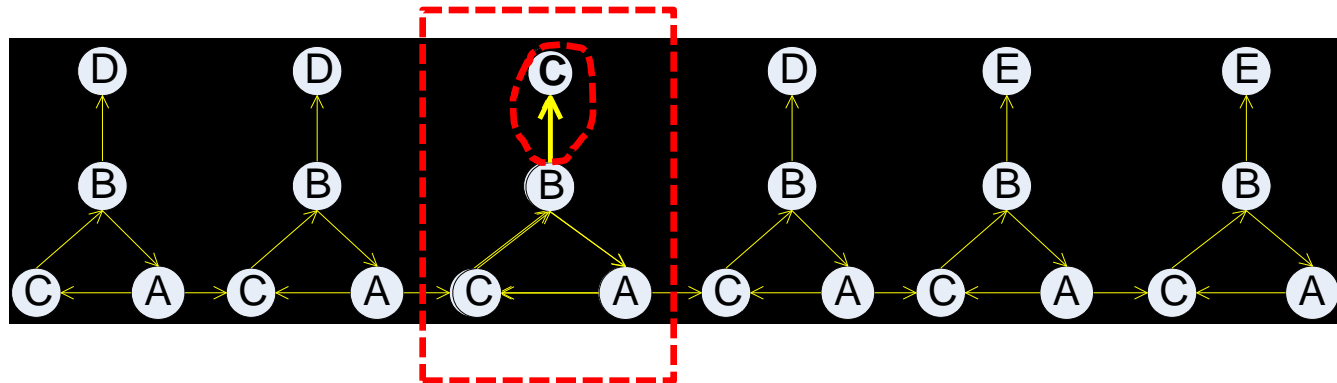


## 2) Probabilistic Approach

- Find normative substructure **S**
- Find extensions to **S** with **lowest probability**
- For each extension  $I_k$  of **S**

$$\text{anomalyScore}(I_k) = \frac{\text{number of instances of } I_k}{\text{all instances } I_n \text{ with a unique extension}}$$

- **Example:**



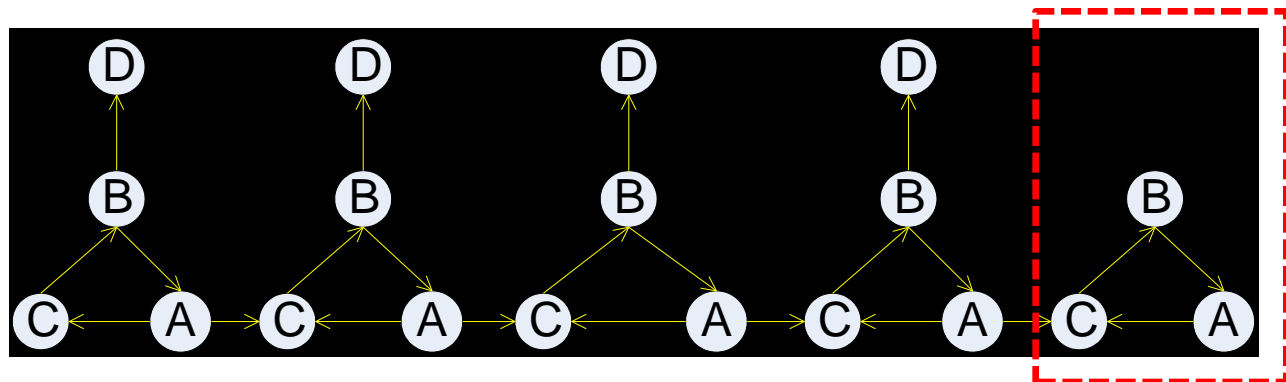
# 3) Maximum Partial Substructure Approach

- Find normative substructure **S**
- Find “ancestral” substructures  $S_n \subseteq S$  that are **missing** various edges and vertices.
- For each instance  $I_k$  of **S<sub>n</sub>**

$$\text{anomalyScore}(I_k) = |I_k| * \text{matchcost}(I_k, S)$$

# instances of  $I_k$  ↗

- Example:**



# Experiments (Cargo shipments)

- **Data:** obtained from Customs and Borders Protection (CBP)
- **Scenario:**
  - Marijuana seized at Florida port [press release by U.S. Customs Service, 2000].
  - Smuggler did not disclose some financial information, and ship traversed extra port.
  - **GBAD-P discovers the extra traversed port;**
  - **GBAD-MPS discovers the missing financial info.**



# Experiments (Network intrusion)

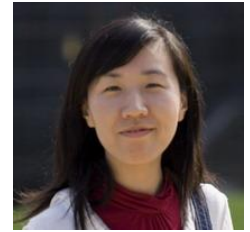


- **Data:** 1999 KDD Cup Network Intrusion
  - 100% of attacks were discovered with GBAD-MDL
  - 55.8% for GBAD-P and 47.8% for GBAD-MPS

## Note

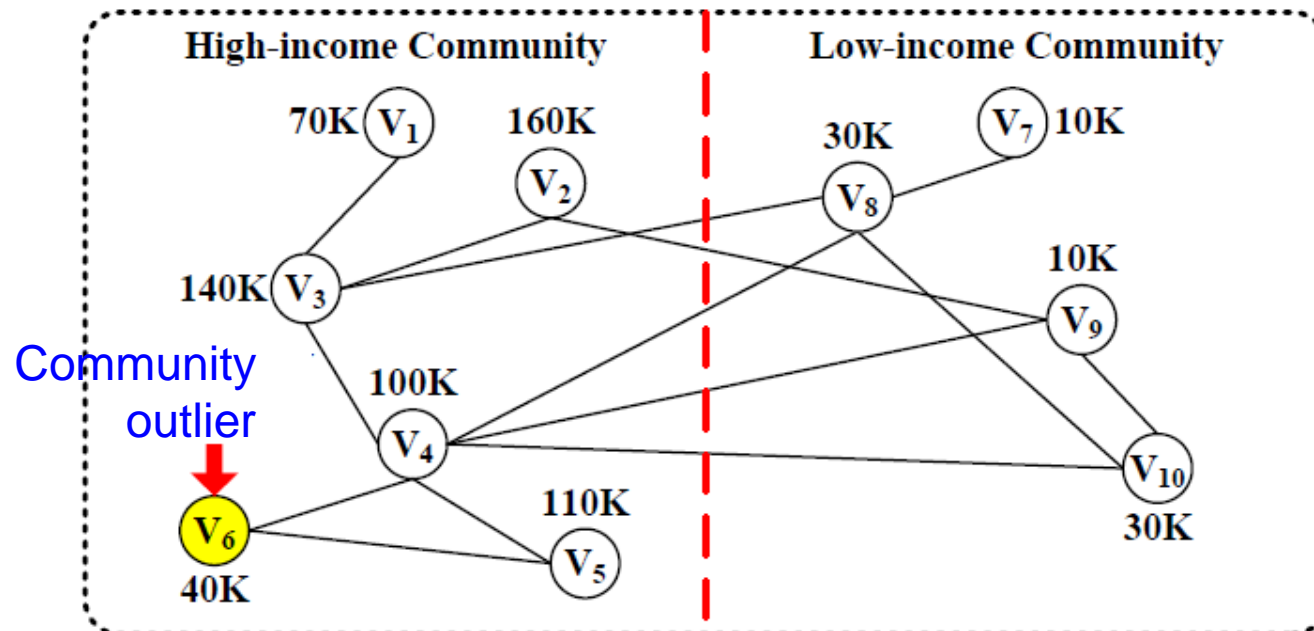
- Data consists of TCP packets that have fixed size
- Thus, the inclusion of additional structure, or the removal of structure, is not relevant here.
- **Modification is the only relevant one**, at which GBAD-MDL performs well
- **High (unreported) false positive rate!**

# Community Outliers



## ■ Definition

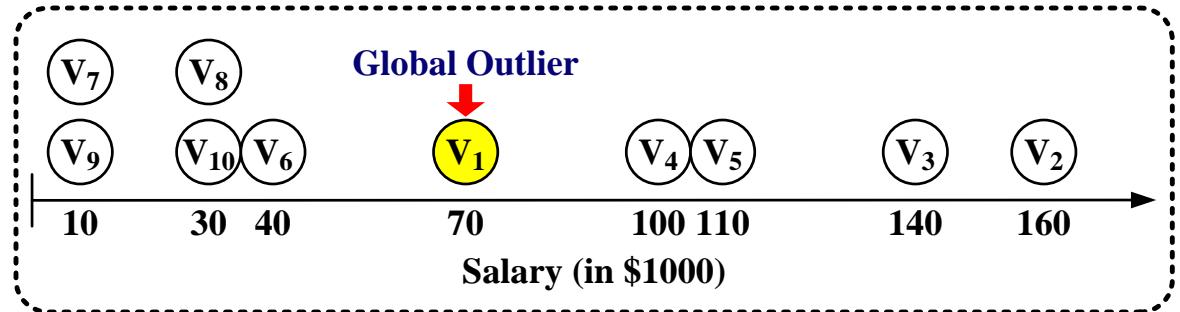
- Two information sources: **links**, **node features**
- **Communities based on both** links and node features
- Objects with features deviating from other community members defined as **community outliers**





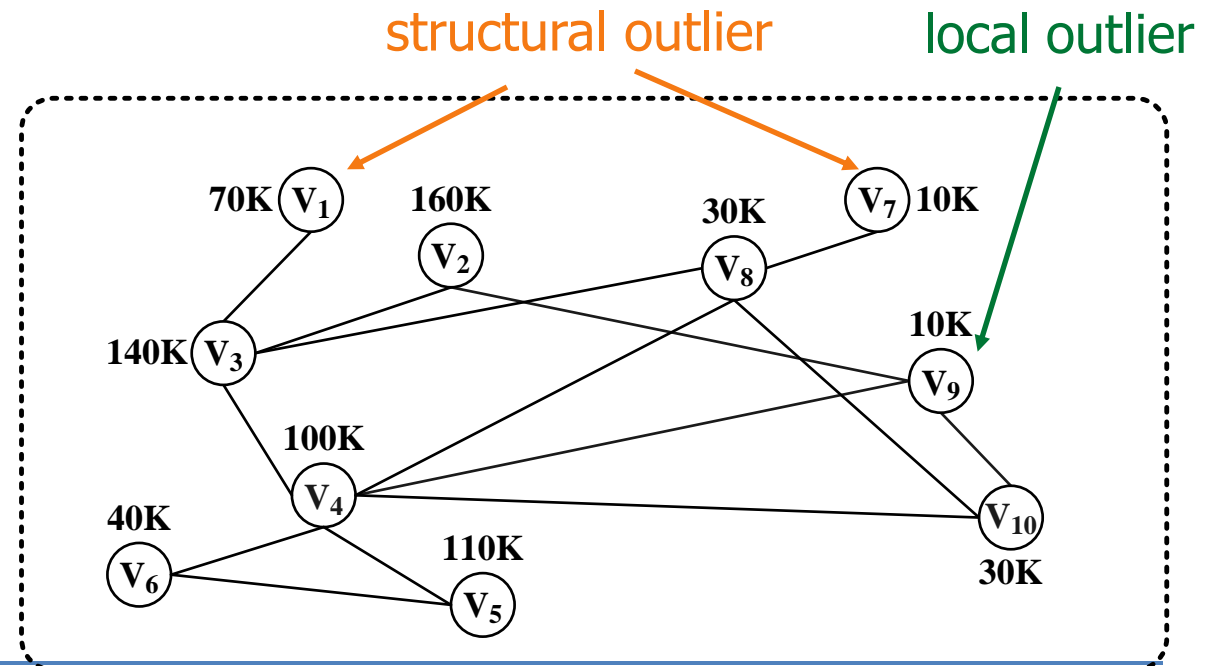
# Other network outliers

1) Global outlier:  
only considers  
node features

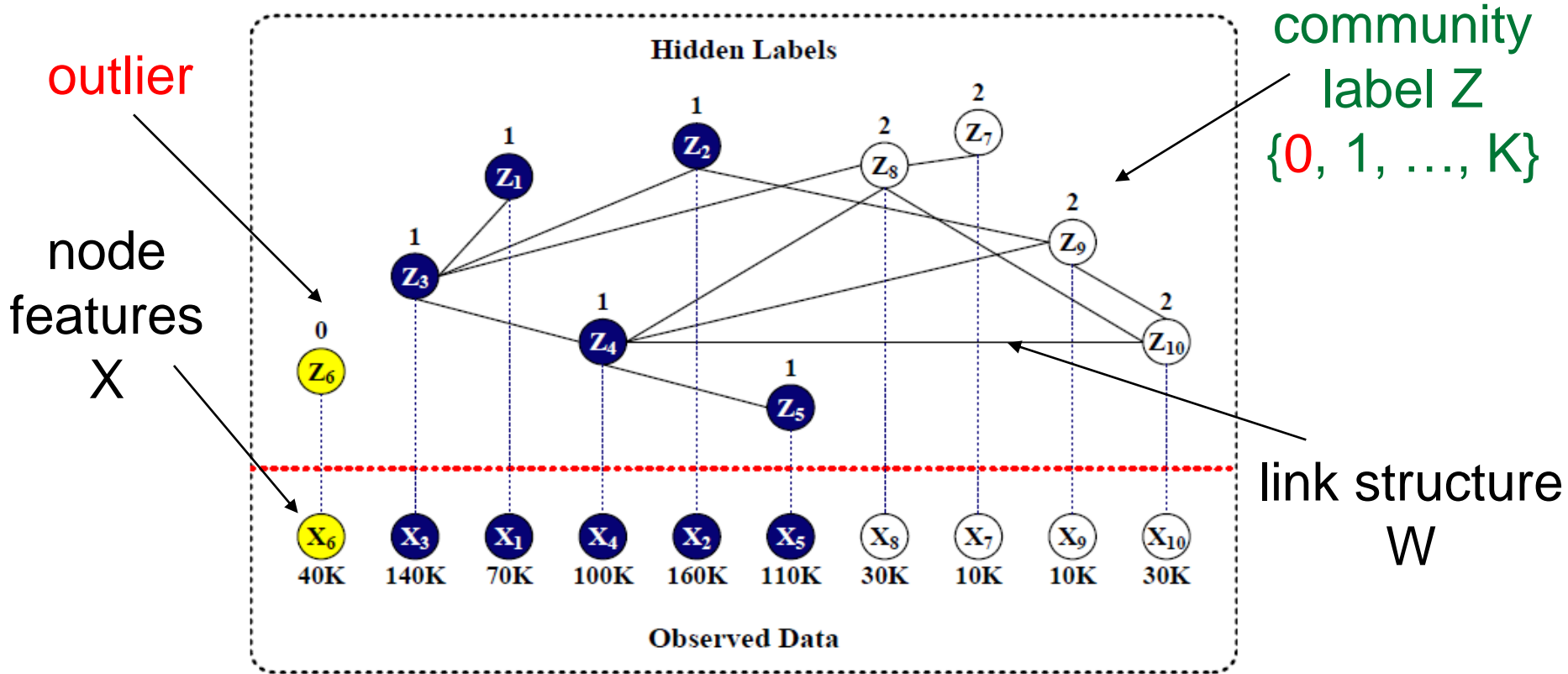


2) Structural outlier:  
only consider links

3) Local outlier:  
only consider the  
feature values of  
direct neighbors



# A unified probabilistic model



$$\Theta = (\theta_1, \dots, \theta_K)$$

K: number of communities  
(user input)

model parameters  
X's are drawn from

# Optimization formulation

- Maximize  $P(X) \propto P(X|Z) P(Z)$ 
  - $P(X|Z)$  depends on community label and model param.s
    - e.g., salaries in the high or low-income communities follow Gaussian distributions defined by mean and std

$$P(x_i = s_i | z_i = k) = P(x_i = s_i | \theta_k)$$

$$P(x_i = s_i | z_i = 0) = \rho_0$$

Normal with  $\{\mu_k, \sigma_k^2\}$

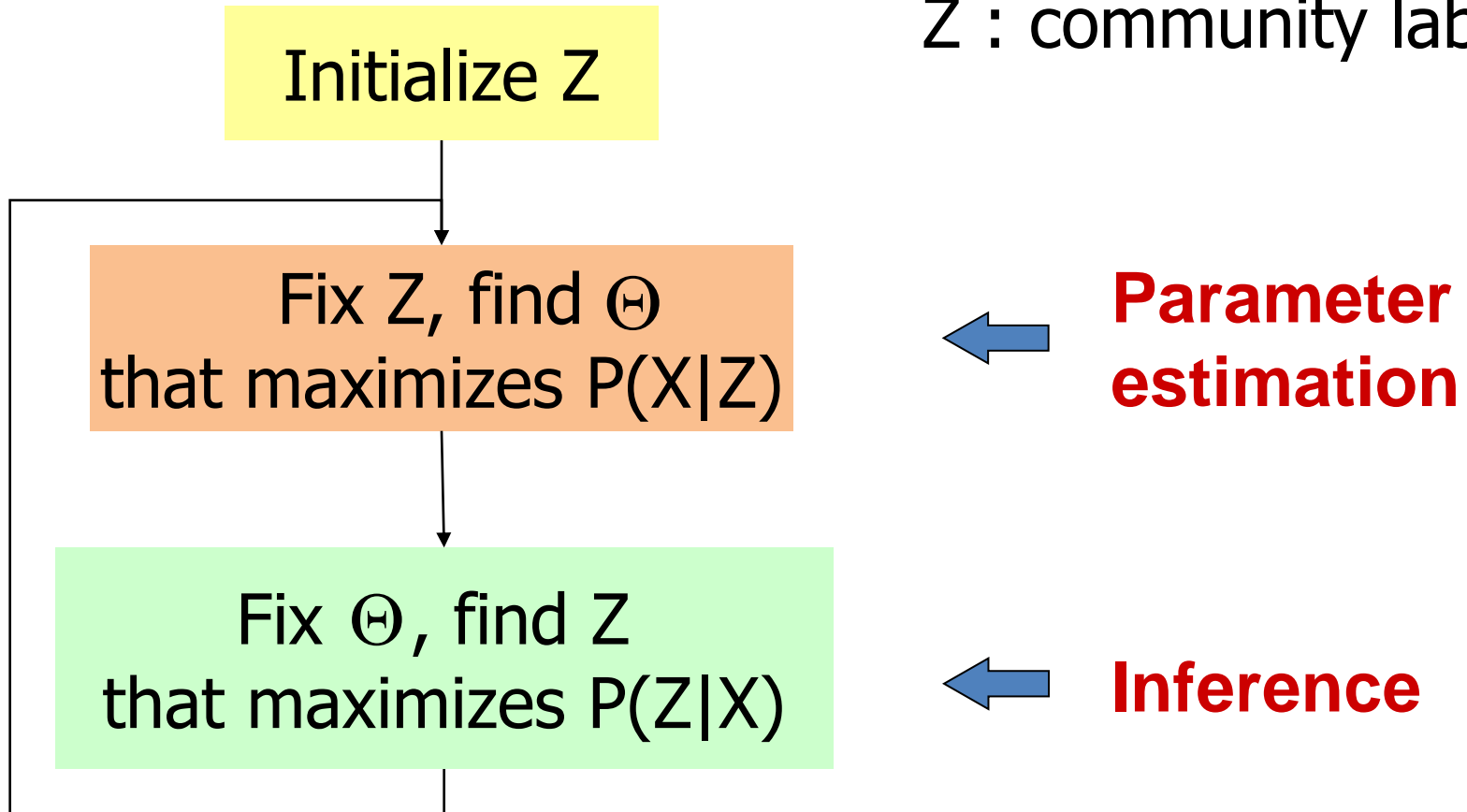
Uniform for outliers

- $P(Z)$  is higher if neighboring nodes from normal communities share the same community label
  - e.g., two linked nodes are likely to be in the same community
  - outliers are isolated—does not depend on the labels of neighbors

$$P(Z) \propto \sum_{w_{ij} > 0, z_i \neq 0, z_j \neq 0} w_{ij} \delta(z_i - z_j)$$

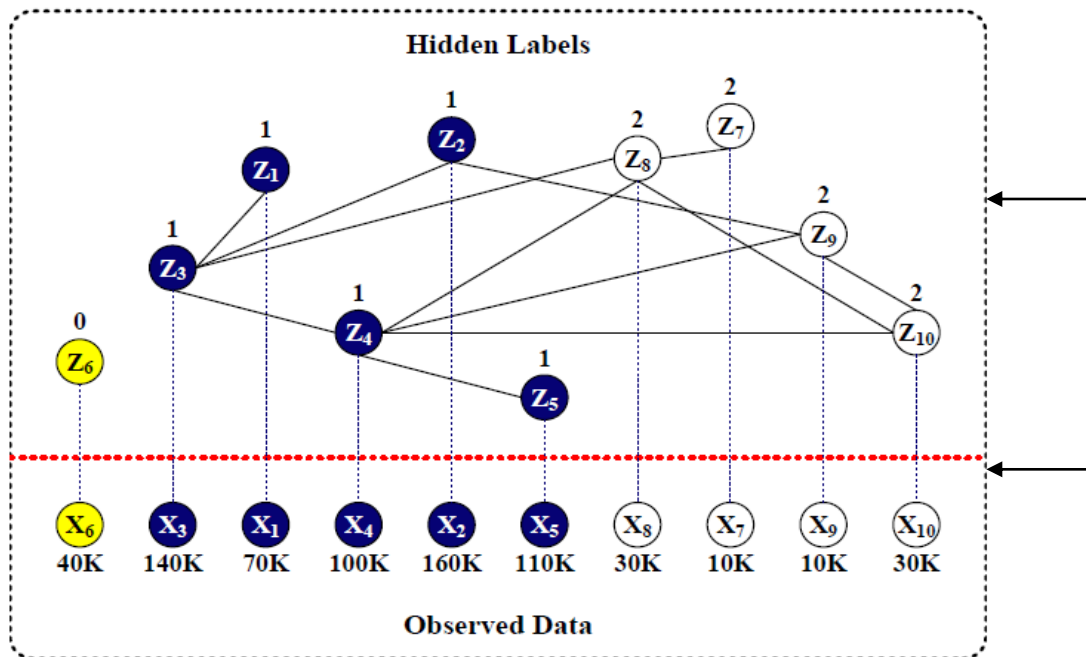
# Algorithm

$\Theta$  : model parameters  
 $Z$  : community labels



# Algorithm: parameter estimation

- Calculate model parameters  $\Theta$ 
  - maximum likelihood estimation
- Continuous:  $\{\mu_k, \sigma_k^2\}$ 
  - mean: sample mean of the community
  - std: square root of sample variance of community



high-income:  
mean: 116k  
std: 35k

low-income:  
mean: 20k  
std: 12k

# Algorithm: Inference

## ■ Calculate label assignments $\mathbf{z}$

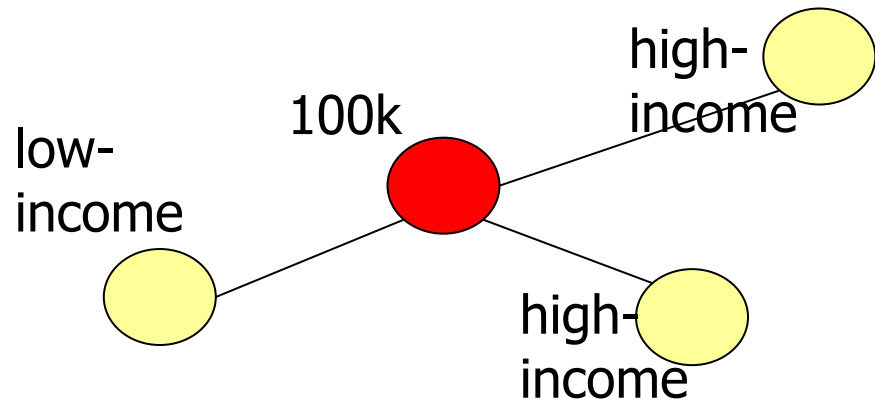
- Model parameters are known
- **Iteratively** update the community labels of nodes
- For each node: select label that maximizes:

high-income:  
mean: 116k  
std: 35k

low-income:  
mean: 20k  
std: 12k

$$P(z_i | x_i = s_i, z_{I-\{i\}}) \propto P(x_i = s_i | z_i) \cdot \exp\left(\lambda \sum_{j \in N_i} w_{ij} \delta(z_i - z_j)\right)$$

high-income:	$P(\text{salary}=100\text{k}   \text{high-income})$	$P(\text{high-income}   \text{neighbors})$
low-income:	$P(\text{salary}=100\text{k}   \text{low-income})$	$P(\text{low-income}   \text{neighbors})$
outlier:	constant	



# Experiments: Simulations

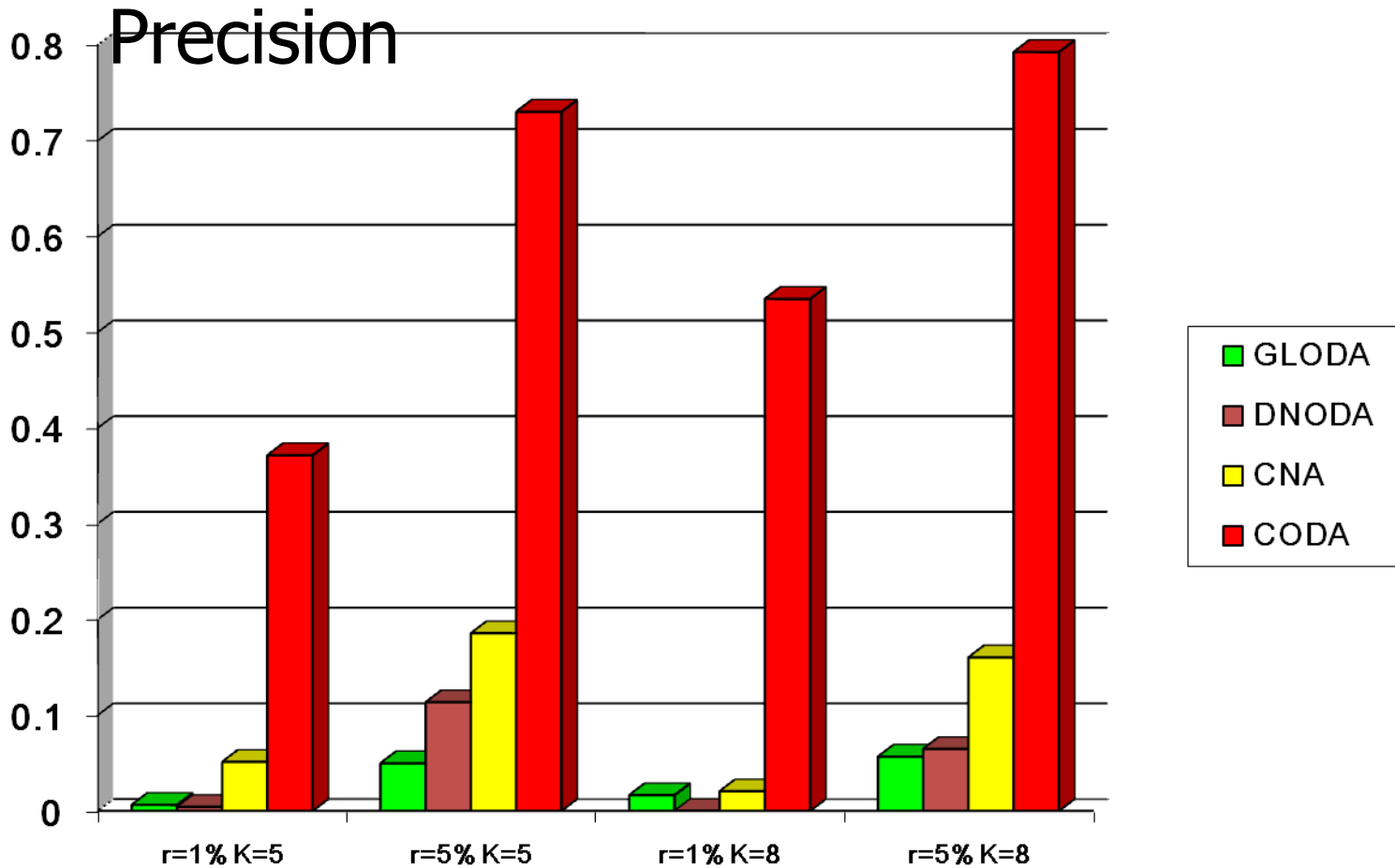
## ■ Data

- Generate continuous data based on Gaussian distributions and generate labels according to the model
- $r$ : percentage of outliers,  $K$ : number of communities

## ■ Baseline models

- **GLODA**: global outlier detection (based on node features only)
- **DNODA**: local outlier detection (check the feature values of direct neighbors)
- **CNA**: partition data into communities based on links and then conduct outlier detection in each community

# Experiments: Simulations





# Case study on DBLP

- Conferences graph
  - Links: % common authors among two
  - Node features: publication titles in the conference

- Communities:

- Database: ICDE, VLDB, SIGMOD, PODS, EDBT
- Artificial Intelligence: IJCAI, AAAI, ICML, ECML
- Data Mining: KDD, PAKDD, ICDM, PKDD, SDM
- Information Analysis: SIGIR, WWW, ECIR, WSDM

- Community outliers: CVPR and CIKM

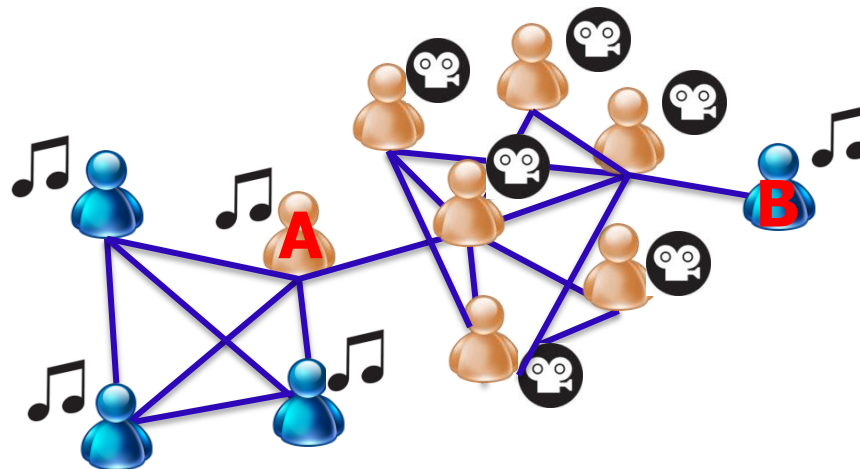
# Cohesive groups in attributed graphs

## ■ Problem:

**Given** a graph with node attributes (features)

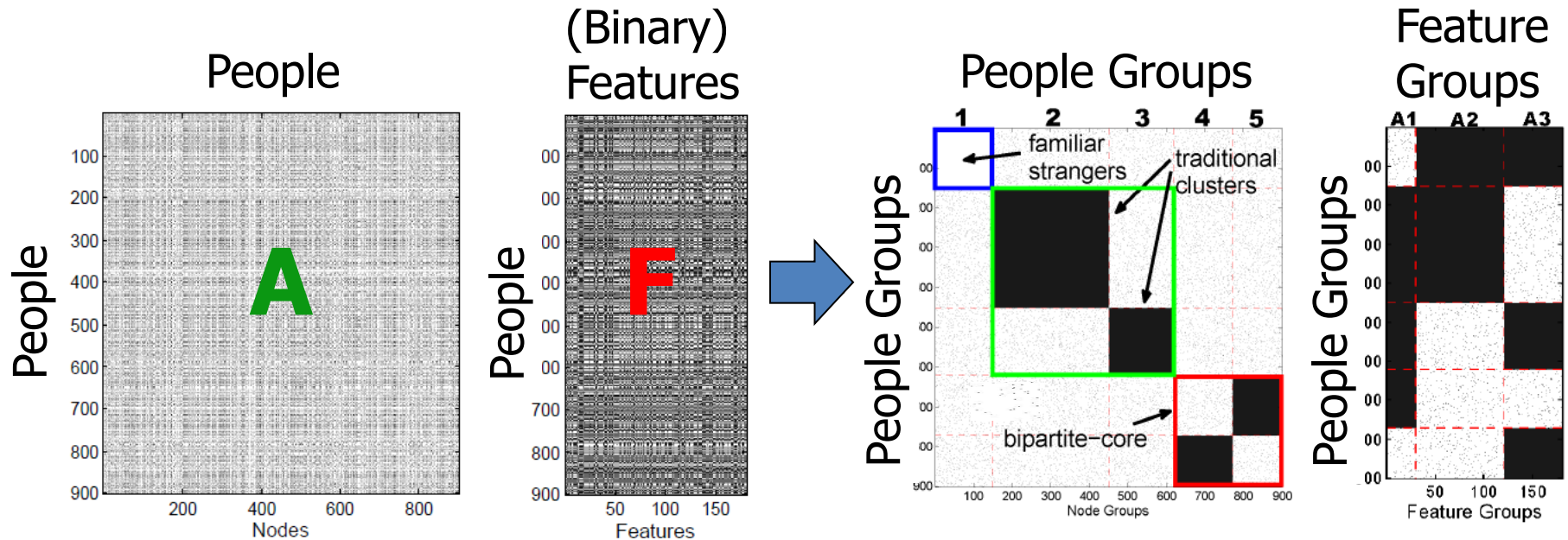
- social networks + user interests
- phone call networks + customer demographics
- gene interaction networks + gene expression info

**Find** cohesive clusters, bridges, anomalies



**Note:** cohesive cluster: similar connectivity & attributes

# Problem sketch



**Given** adjacency matrix  $A$  and feature matrix  $F$   
**Find** homogeneous blocks (clusters) in  $A$  and  $F$

- \* parameter-free
- \* scalable

# Problem formulation

1. How many node- & attribute-clusters?
2. How to assign nodes and attributes to clusters?

**Main idea:** employ Minimum Description Length

$$\underbrace{L(M)} + \underbrace{L(D|M)}$$

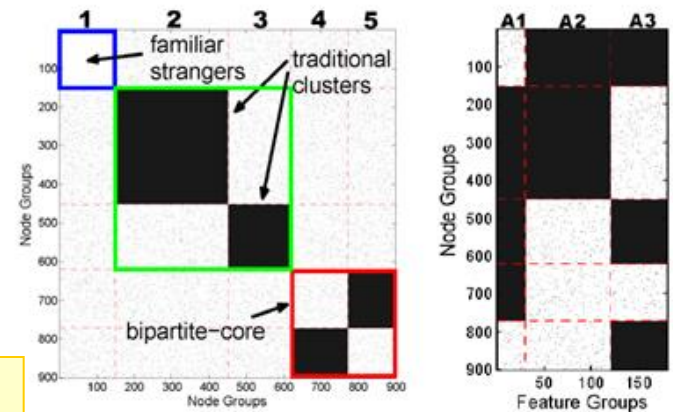
encoding length  
of clustering

encoding length  
of blocks

Good  
Clustering



Good  
Compression





# Problem formulation

- $L(M)$  : Model description cost

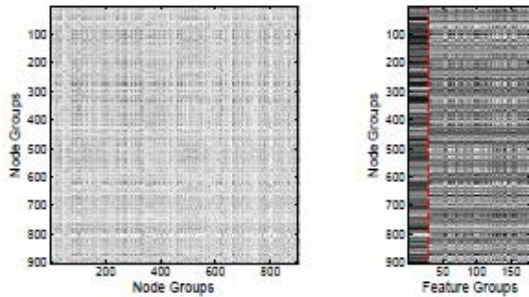
1.  $\log^* n + \log^* f$        $n$ : #nodes,  $f$ : #attributes
2.  $\log^* k + \log^* l$        $k$ : #node-clusters,  $l$ : #attribute-clusters
3.  $nH(P) + fH(Q)$ 
  - $p_i = \frac{r_i}{n}$  ← size of node-cluster  $i$
  - $q_j = \frac{c_j}{f}$  ← size of attribute-cluster  $j$

- $L(D|M)$ : Data description cost given Model

1. For each block in  $A$  and  $F$ , #1s:  $\log^* n_1(B_{ij})$
2.  $E(B_{ij}) = -n_1(B_{ij}) \log_2(P_{ij}(1)) - n_0(B_{ij}) \log_2(P_{ij}(0))$

A similar problem (column re-ordering for minimum total run length) is shown to be NP-hard [Johnson+].  
(reduction from Hamiltonian Path)

# Algorithm sketch



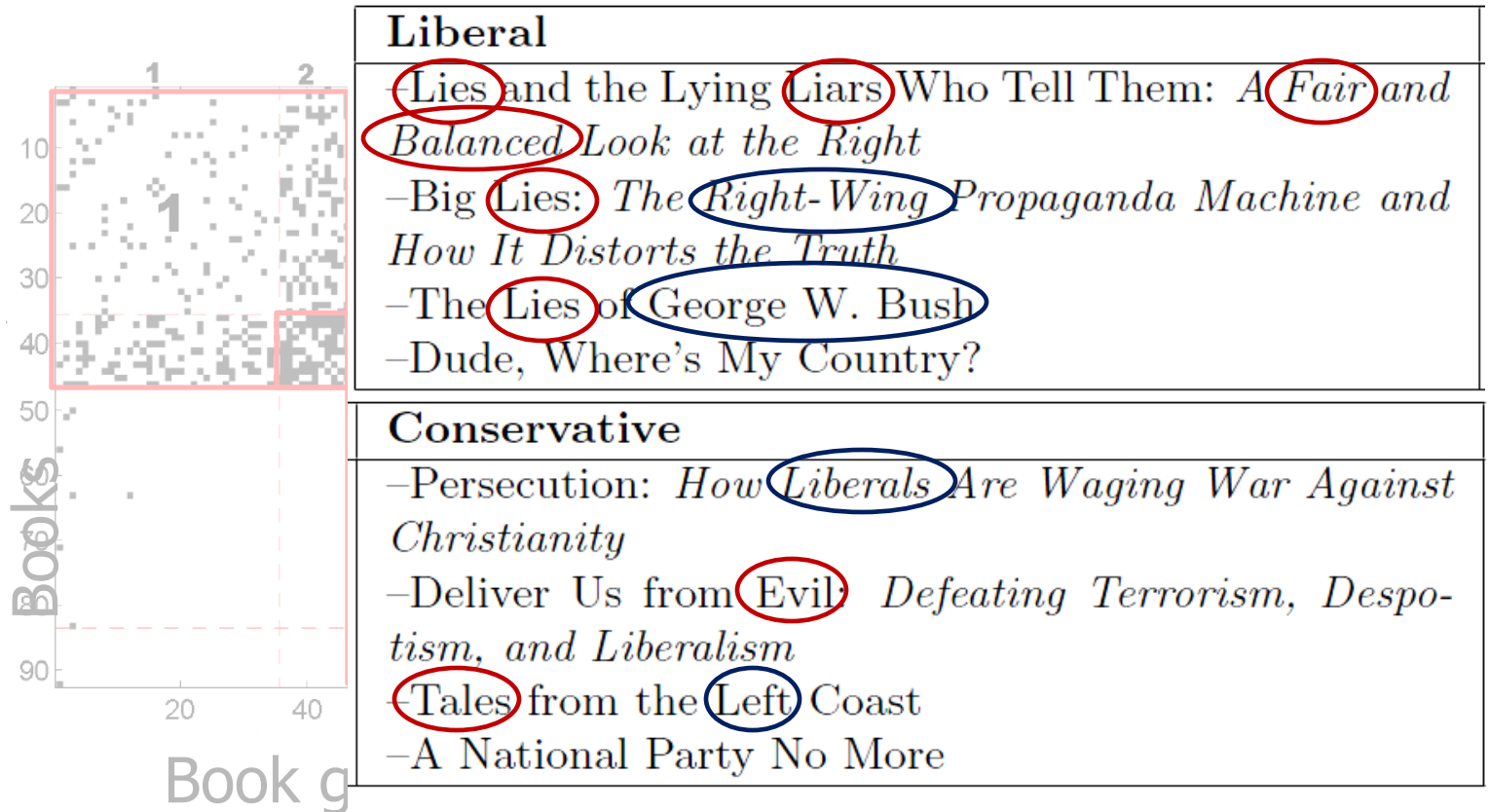
(a)  $k=1$   $l=2$   
Split-FeatureGroup



The algorithm is iterative and monotonic  
–will converge to local optimum

# PICS at work (Political books)

## Examples of “core” liberal and conservative books

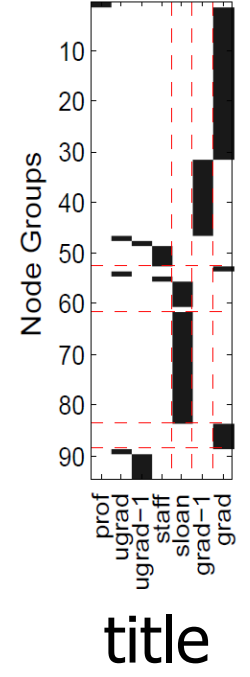
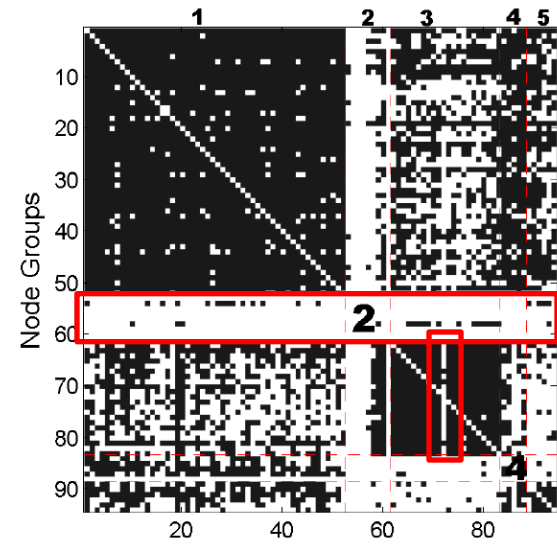
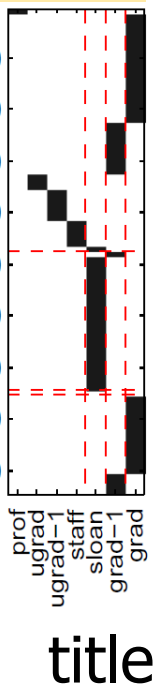
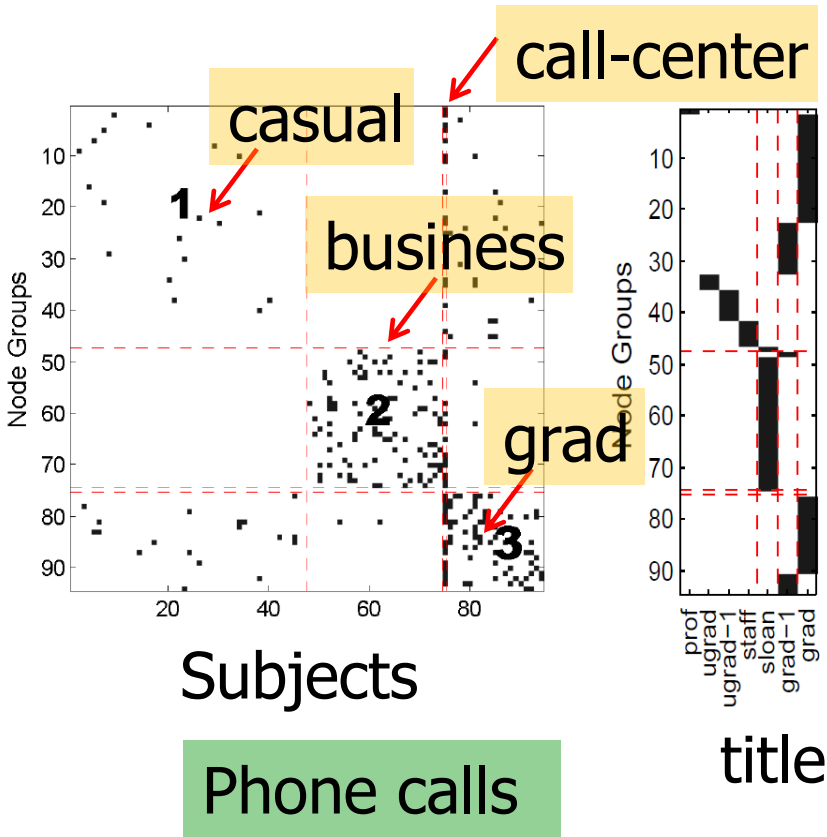


## Examples of bridging ‘conservative’ books

“core and periphery”

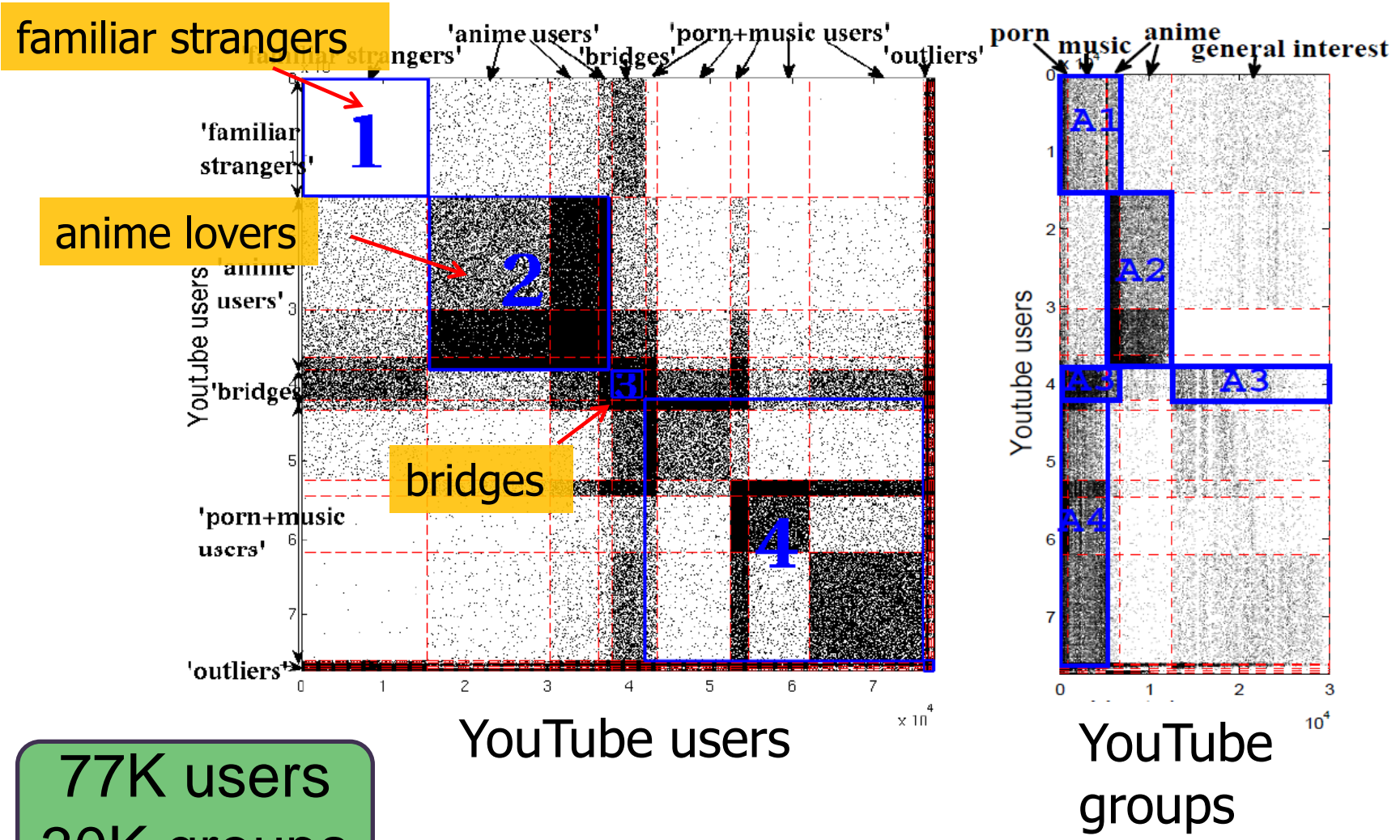
- *Bush at War*
- *The Bushes: Portrait of a Dynasty*
- *Rise of the Vulcans: The History of Bush's War Cabinet*

# PICS at work (Reality mining)





# PICS at work (YouTube)



77K users  
30K groups

# Part I: References (attribute graphs)

- C. C. Noble and D. J. Cook. [Graph-based anomaly detection](#). KDD, pages 631–636, 2003.
- W. Eberle and L. B. Holder. [Discovering structural anomalies in graph-based data](#). ICDM Workshops, pages 393–398, 2007.
- Michael Davis, Weiru Liu, Paul Miller, George Redpath: [Detecting anomalies in graphs with numeric labels](#). 1197-1202, CIKM 2011.
- Jing Gao, Feng Liang, Wei Fan, Chi Wang, Yizhou Sun, Jiawei Han: [On community outliers and their efficient detection in information networks](#). KDD 2010: 813-822.
- Leman Akoglu, Hanghang Tong, Brendan Meeder, Christos Faloutsos. [PICS: Parameter-free Identification of Cohesive Subgroups in large attributed graphs](#). SDM, 2012.

# Tutorial Outline

- Motivation, applications, challenges
- **Part I:** Anomaly detection in **static** data
  - Overview: Outliers in **clouds of points**
  - Anomaly detection in **graph data**
- ➔ **Part II:** Event detection in **dynamic** data
  - Overview: Change detection in **time series**
  - Event detection in **graph sequences**
- **Part III:** Graph-based **algorithms and apps**
  - Algorithms: **relational learning**
  - Applications: **fraud and spam** detection

# Coffee break...

